Reasoning with Expressive Description Logics: Theory and Practice

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Reasoning with Expressive DLs - p.1/39

Introduction to Description Logics (DLs)

Introduction to Description Logics (DLs) Reasoning techniques

Introduction to Description Logics (DLs) Reasoning techniques Implementing DL systems

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- Key features of DLs are
 - Well defined semantics (they are logics)
 - Provision of inference services

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Classic system used to configure telecom equipment

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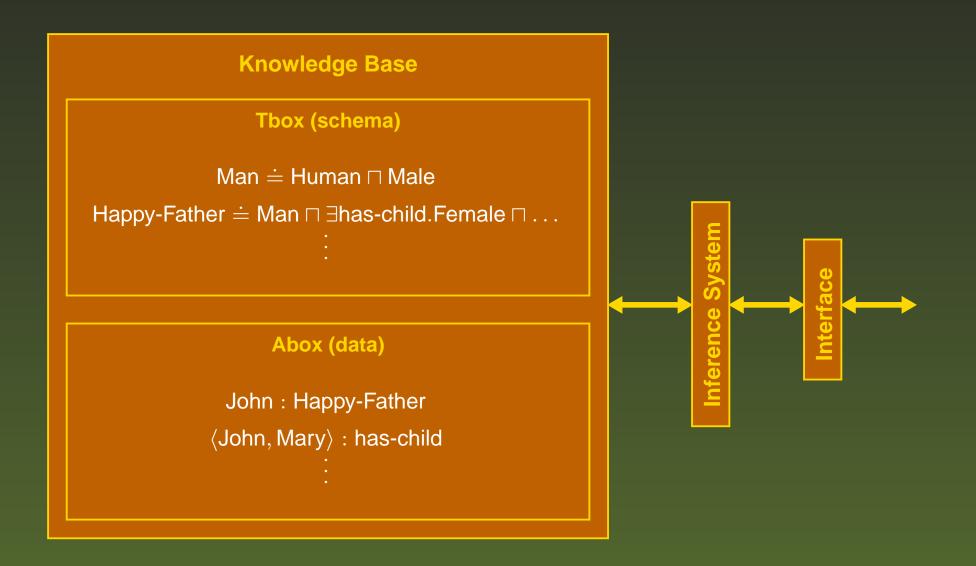
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Database schema and query reasoning

- Schema design and query optimisation
- Interoperability and federation
- Query containment (w.r.t. schema)

DL System Architecture



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- $<\!\!\!<\!\!\!<$ This basic DL is known as \mathcal{ALC}

For example, concept Happy Father in ALC:

- Man \square \exists has-child.Male
 - \sqcap \exists has-child.Female
 - \sqcap \forall has-child.(Doctor \sqcup Lawyer)

DL Syntax and Semantics

Semantics given by interpretation $\mathcal{I} = (\Delta^{\mathcal{I}}, \cdot^{\mathcal{I}})$

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Constructor	Syntax	Example	Semantics		
atomic concept	A	Human	$A^{\mathcal{I}} \subseteq \Delta^{\mathcal{I}}$		
atomic role	R	has-child	$R^{\mathcal{I}} \subseteq \Delta^{\mathcal{I}} \times \Delta^{\mathcal{I}}$		
and for C , D concepts and R a role name					
conjunction	$C\sqcap D$	Human \sqcap Male $C^{\mathcal{I}} \cap D^{\mathcal{I}}$			
disjunction	$C \sqcup D$	Doctor ⊔ Lawyer	$C^{\mathcal{I}} \cup D^{\mathcal{I}}$		
negation	$\neg C$	⊸Male	$\Delta^{\mathcal{I}} \setminus C$		
exists restr.	$\exists R.C$	∃has-child.Male	$\{x \mid \exists y. \langle x, y \rangle \in R^{\mathcal{I}} \land y \in C^{\mathcal{I}}\}$		
value restr.	$\forall R.C$	∀has-child.Doctor	$ \{x \mid \forall y. \langle x, y \rangle \in R^{\mathcal{I}} \implies y \in C^{\mathcal{I}} \} $		

Other DL Constructors

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Constructor	Syntax	Example	Semantics
number restr.	$\geqslant nR$	≥3 has-child	$ \{x \mid \{y.\langle x, y\rangle \in R^{\mathcal{I}}\} \geqslant n\} $
	$\leqslant nR$	$\leqslant 1$ has-mother	$\{x \mid \{y.\langle x, y\rangle \in R^{\mathcal{I}}\} \leqslant n\}$
inverse role	R^{-}	has-child $^-$	$\{\langle x,y\rangle\mid \langle y,x\rangle\in R^{\mathcal{I}}\}$
trans. role	R^*	has-child*	$(R^{\mathcal{I}})^*$
concrete domain	$f_1,\ldots,f_n.P$	earns spends <	$\{x \mid P(f_1^{\mathcal{I}}, \dots, f_n^{\mathcal{I}})\}$

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Inclusion (GCI) axioms assert subsumption relations $C \sqsubseteq D$ (note $C \doteq D$ equivalent to $C \sqsubseteq D$ and $D \sqsubseteq C$) \exists has-degree.Masters $\sqsubseteq \exists$ has-degree.Bachelors

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An interpretation \mathcal{I} satisfies $C \doteq D$ iff $C^{\mathcal{I}} = D^{\mathcal{I}}$ $C \sqsubseteq D$ iff $C^{\mathcal{I}} \subseteq D^{\mathcal{I}}$ A **Tbox** \mathcal{I} iff it satisfies every axiom in \mathcal{I} ($\mathcal{I} \models \mathcal{I}$)

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DL Knowledge Base (Abox)

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An interpretation *I* satisfies

a: C iff $a^{\mathcal{I}} \in C^{\mathcal{I}}$ $\langle a, b \rangle : R$ iff $\langle a^{\mathcal{I}}, b^{\mathcal{I}} \rangle \in R^{\mathcal{I}}$ An Abox \mathcal{A} iff it satisfies every axiom in \mathcal{A} ($\mathcal{I} \models \mathcal{A}$) A KB $\Sigma = \langle \mathcal{T}, \mathcal{A} \rangle$ iff it satisfies both \mathcal{T} and \mathcal{A} ($\mathcal{I} \models \Sigma$)

Basic Inference Problems

Subsumption (structure knowledge, compute taxonomy) $C \sqsubseteq D$? Is $C^{\mathcal{I}} \subseteq D^{\mathcal{I}}$ in all interpretations? **Subsumption** (structure knowledge, compute taxonomy) $C \subseteq D$? Is $C^{\mathcal{I}} \subseteq D^{\mathcal{I}}$ in all interpretations?

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Is C consistent w.r.t. \mathcal{T} ? Is there a model \mathcal{I} of \mathcal{T} s.t. $C^{\mathcal{I}} \neq \emptyset$?

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Problems are **closely related**:

 $C \sqsubseteq_{\mathcal{T}} D$ iff $C \sqcap \neg D$ is inconsistent w.r.t. \mathcal{T} C is consistent w.r.t. \mathcal{T} iff $C \not\sqsubseteq_{\mathcal{T}} A \sqcap \neg A$

Reasoning Techniques

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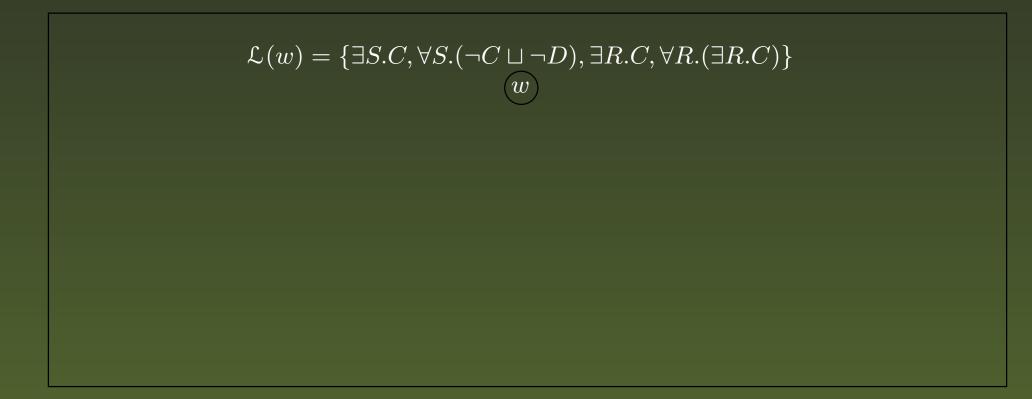
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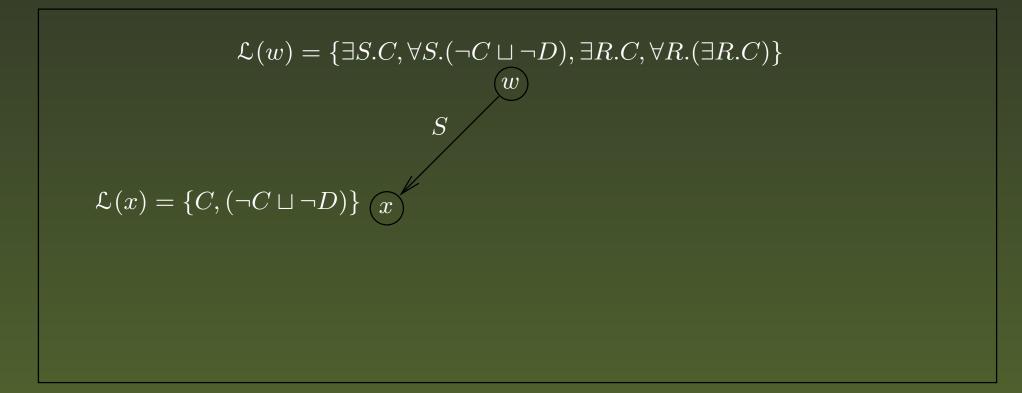
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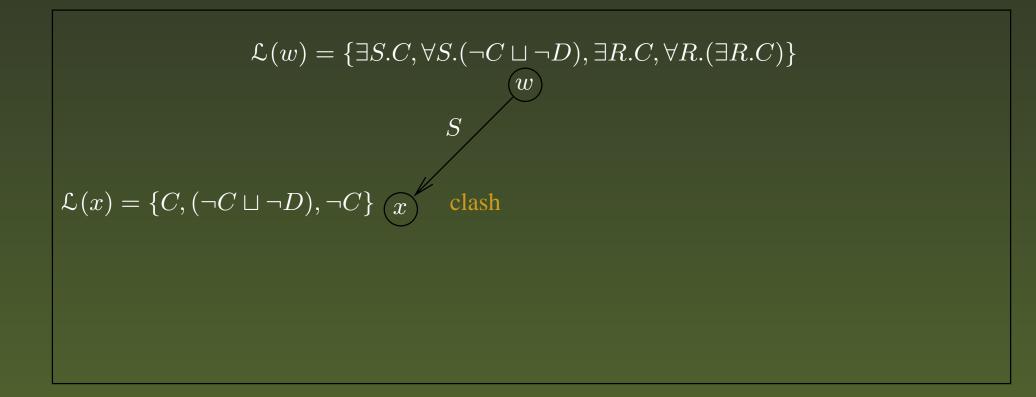
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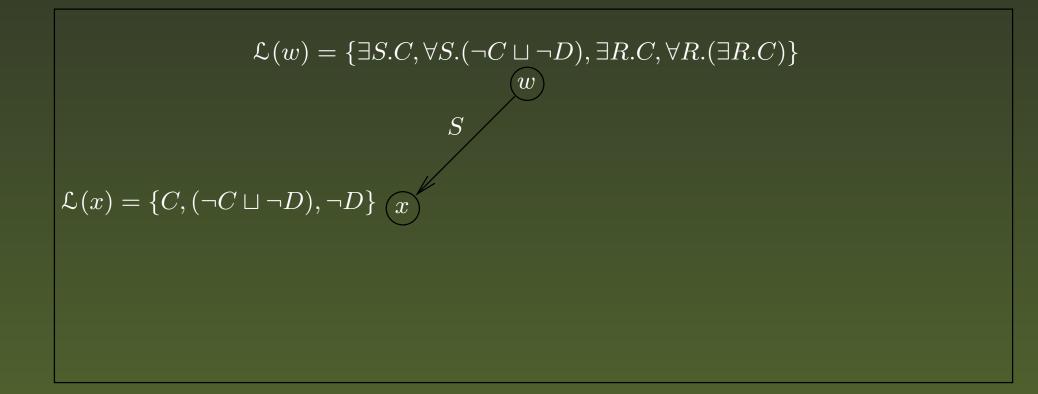
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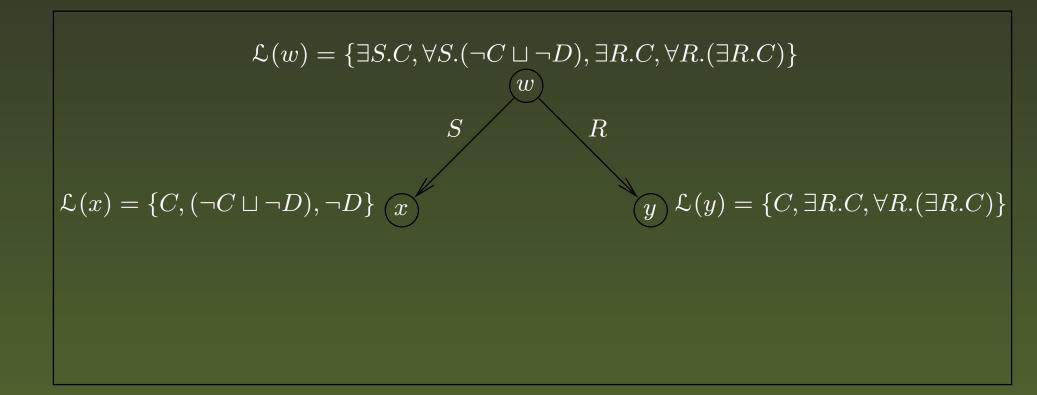
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 - Blocking ensures termination (with expressive DLs)

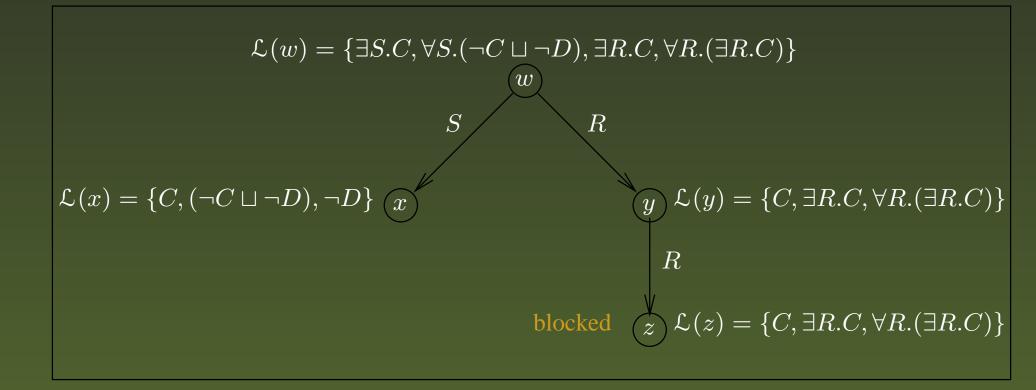


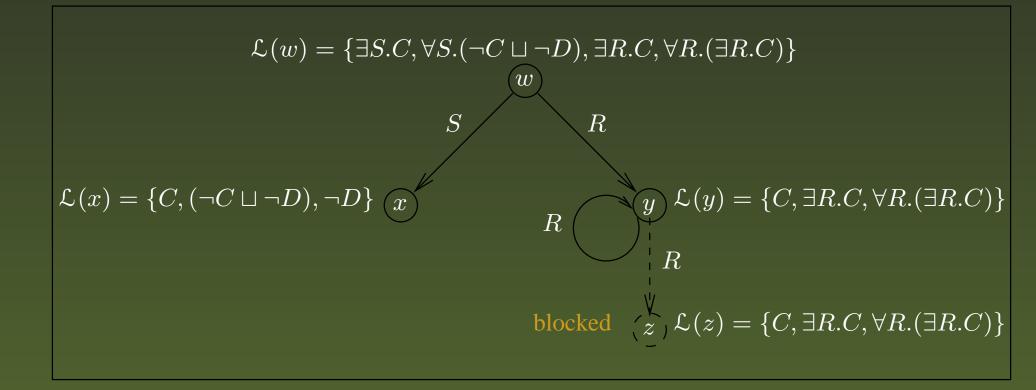












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- Forest instead of Tree (for Aboxes)

Implementing DL Systems

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- **BUT** even simple domain encoding is **disastrous** with large numbers of roles

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 - Small number of hard tests can dominate classification time
 - Recent DL research has addressed this problem (with considerable success)

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 - But often generally applicable to search based algorithms

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- Lexically normalise and simplify all concepts in KB
- Combine with lazy unfolding in tableaux algorithm
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- Structural analysis can discover "obvious" subsumption

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E.g.: {HappyFather, \neg HappyFather} \longrightarrow clash { \forall has-child.(Doctor \sqcup Lawyer), \exists has-child.(\neg Doctor $\sqcap \neg$ Lawyer)} \longrightarrow search

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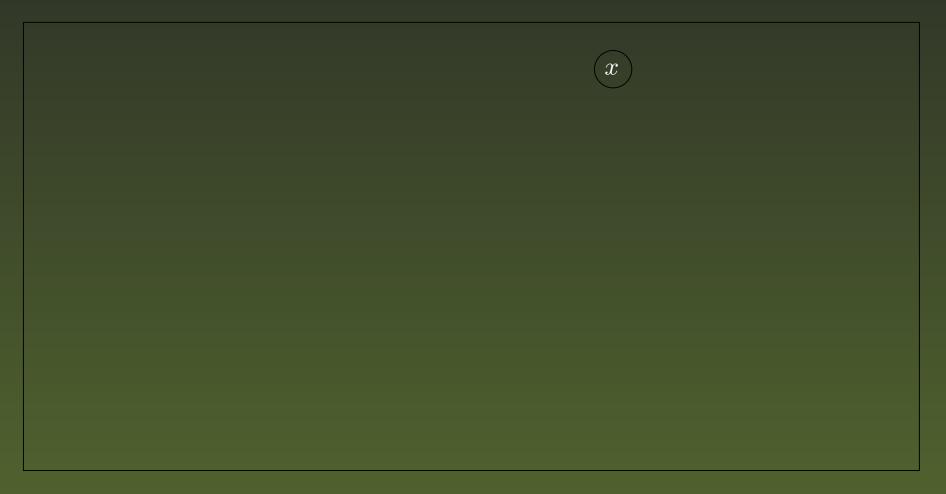
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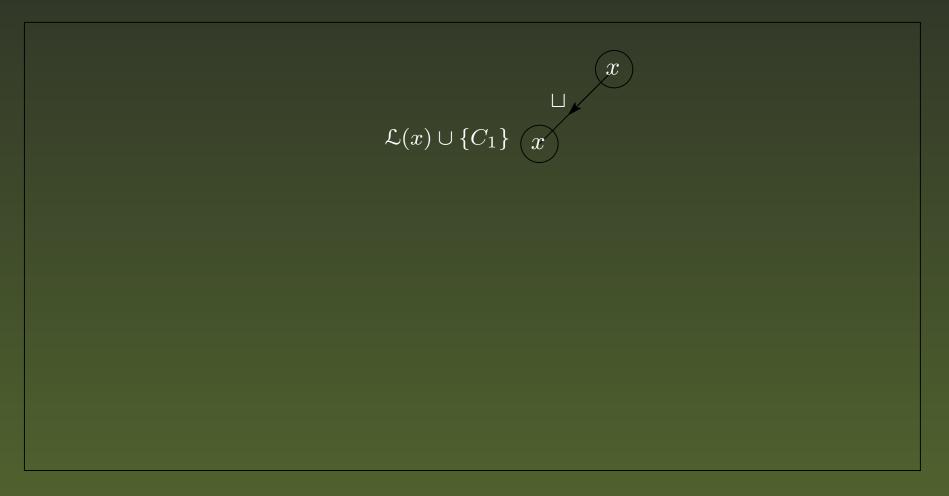
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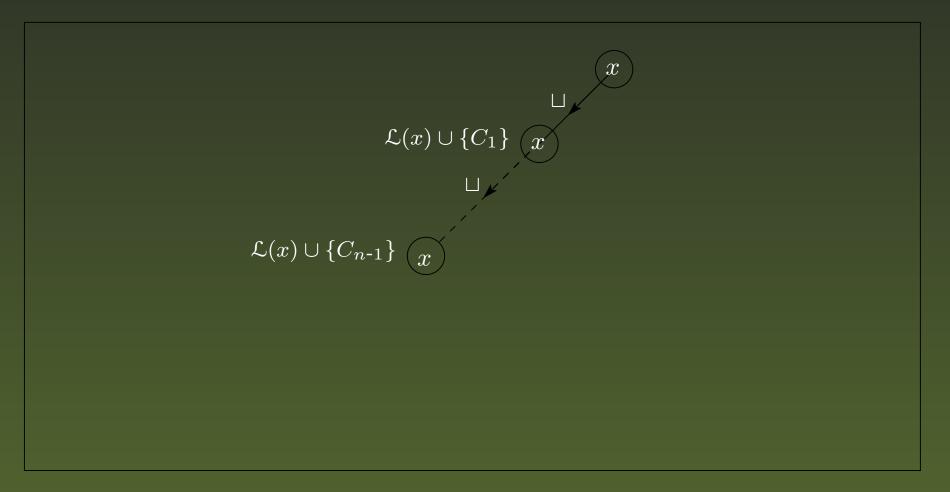
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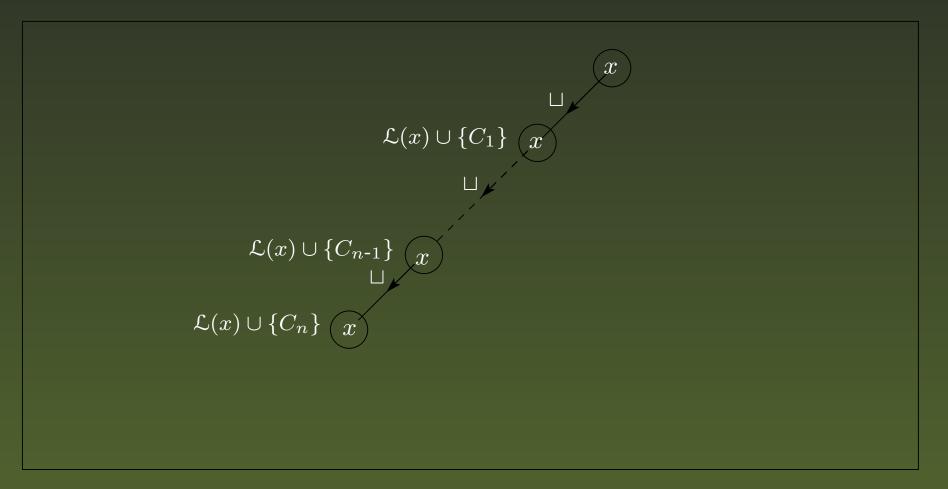
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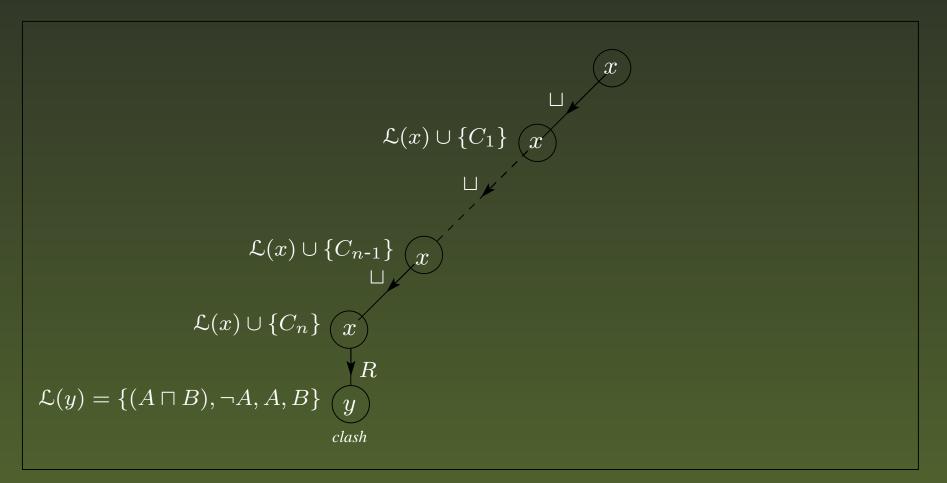
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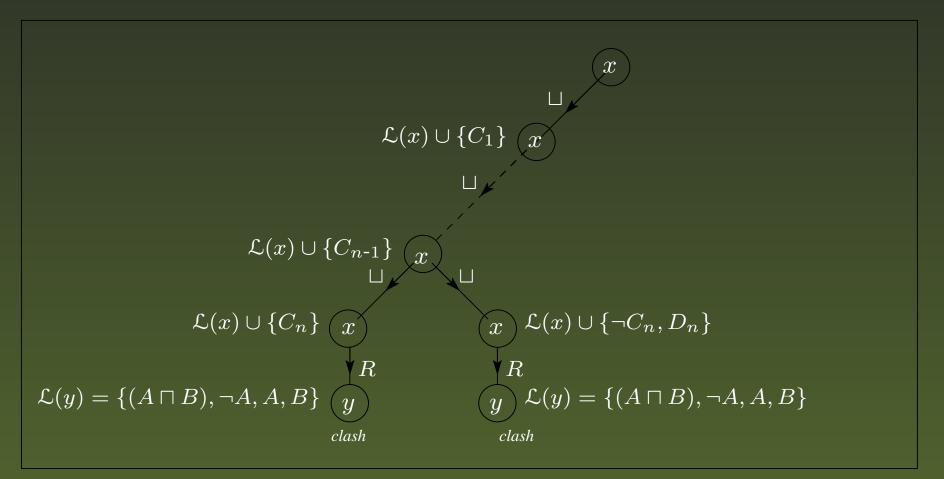


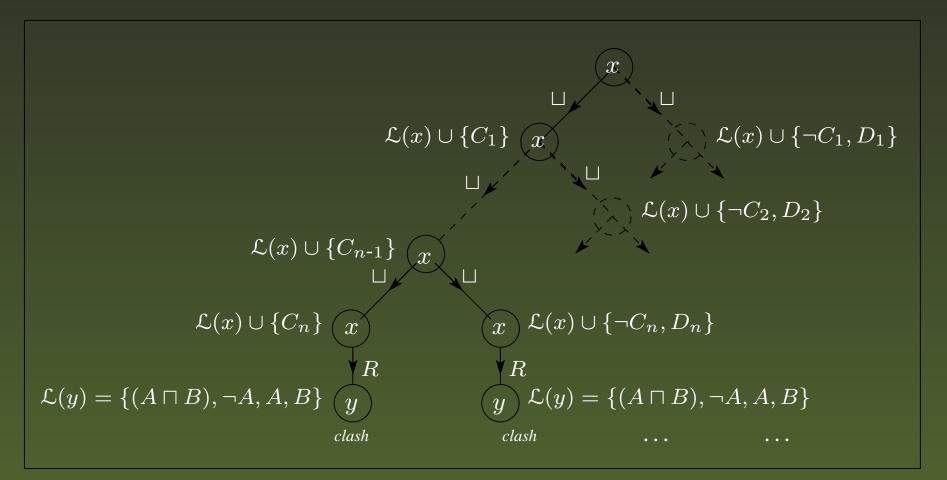


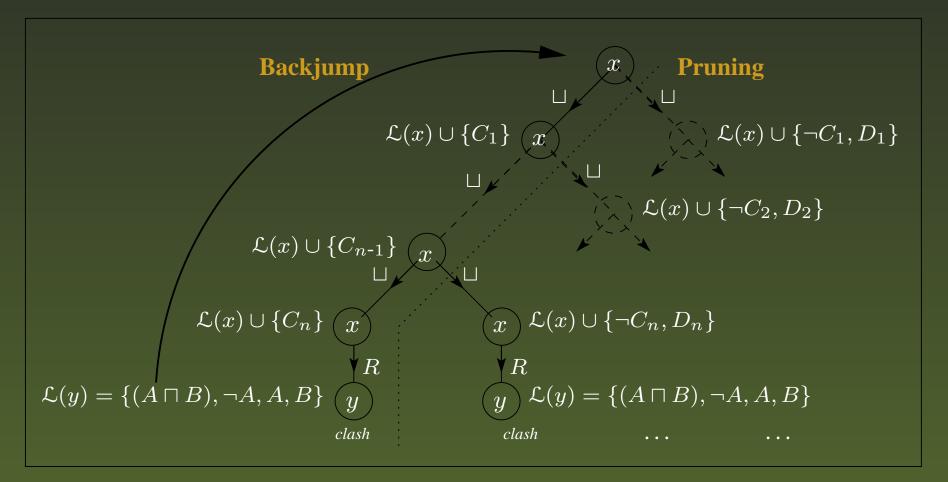
















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DL applications

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 - Use DL classifier to build taxonomy
- Needed expressive DL and efficient reasoning
 - Descriptions use transitive roles, inverses, GCIs etc.
 - Even prototype KB is very large (\approx 3,000 concepts)
 - Existing (incomplete) classifier took ${\approx}24$ hours to classify KB
 - FaCT system (sound and complete) takes \approx 60s

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- E.g., OilEd ontology editor
 - Frame based interface (e.g., Protegé, OntoEdit)
 - Extended to capture whole of OIL/DAML+OIL languages
 - Reasoning support from FaCT (via CORBA interface)



E.g., DAML+OIL medical terminology ontology

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 BloodPressure ⊆ ∃hasValue.(High ⊔ Low) □ ≤1hasValue plus
 High ⊆ ¬Low ⇒ HighLowBloodPressure ⊆ ⊥

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- E.g., I.COM Intelligent Conceptual Modelling tool (Enrico Franconi)
 - Uses FaCT system to provide reasoning support for EER





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 - Web standard ontology language will be DL based

Resources

Slides from this talk

```
www.cs.man.ac.uk/~horrocks/Slides/leipzig-jun-01.pdf
```

FaCT system

```
www.cs.man.ac.uk/fact
```

OIL

```
www.ontoknowledge.org/oil/
```

DAML+OIL

```
www.daml.org/language/
```

OilEd

img.cs.man.ac.uk/oil

I.COM

```
www.cs.man.ac.uk/~franconi/icom/
```

F. Baader, E. Franconi, B. Hollunder, B. Nebel, and H.-J. Profitlich. An empirical analysis of optimization techniques for terminological representation systems or: Making KRIS get a move on. In B. Nebel, C. Rich, and W. Swartout, editors, *Proc. of KR'92*, pages 270–281. Morgan Kaufmann, 1992.

F. Giunchiglia and R. Sebastiani. A SAT-based decision procedure for ALC. In *Proc. of KR'96*, pages 304–314. Morgan Kaufmann, 1996.

V. Haarslev and R. Möller. High performance reasoning with very large knowledge bases: A practical case study. In *Proc. of IJCAI 2001* (to appear).

B. Hollunder and W. Nutt. Subsumption algorithms for concept languages. In *Proc. of ECAI'90*, pages 348–353. John Wiley & Sons Ltd., 1990.

I. Horrocks. *Optimising Tableaux Decision Procedures for Description Logics*. PhD thesis, University of Manchester, 1997.

I. Horrocks and P. F. Patel-Schneider. Comparing subsumption optimizations. In *Proc. of DL'98*, pages 90–94. CEUR, 1998.

I. Horrocks and P. F. Patel-Schneider. Optimising description logic subsumption. *Journal of Logic and Computation*, 9(3):267–293, 1999.

I. Horrocks and S. Tobies. Reasoning with axioms: Theory and practice. In *Proc. of KR'00* pages 285–296. Morgan Kaufmann, 2000.

E. Franconi and G. Ng. The i.com tool for intelligent conceptual modelling. In *Proc. of (KRDB'00)*, August 2000.

D. Fensel, F. van Harmelen, I. Horrocks, D. McGuinness, and P. F. Patel-Schneider. OIL: An ontology infrastructure for the semantic web. *IEEE Intelligent Systems*, 16(2):38–45, 2001.