Description Logic: Axioms and Rules

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Talk Outline



Motivation: The Semantic Web and DAML+OIL

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- W3C Ontology Language WG has taken DAML+OIL as starting point

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- Expressive power determined by
 - Kinds of axiom supported
 - Kinds of class (and property) constructor supported





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 - *SHIQ* is based on 15+ years of DL research
- Can use DL reasoning with DAML+OIL
 - Existing *SHIQ* implementations support (most of) DAML+OIL

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- Ontology integration
 - Assert inter-ontology relationships
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- Ontology deployment
 - Determine if set of facts are consistent w.r.t. ontology
 - Answer queries w.r.t. ontology, e.g., DQL

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 - XML provides syntax transport layer
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- Facilitates provision of reasoning services
 - Known algorithms
 - Implemented systems
 - Evidence of **empirical tractability** (for ontology reasoning)

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 - Boolean connectives (\Box , \sqcup , \neg) and nesting
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 - Fake individuals
- Reasoning support provided by FaCT system
 - Ontology translated into *SHIQ* DL
 - Communicates with FaCT via CORBA interface
 - Indicates inconsistencies and implicit subsumptions

OilEd



Description Logics and Reasoning

What are Description Logics?

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- Also known as terminological logics, concept languages, etc.
- Key features of DLs are
 - Well defined **semantics** (they are logics)
 - Provision of inference services

DL System Architecture



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For example, concept Happy Father in ALC:

- Man \sqcap \exists has-child.Male
 - □ ∃has-child.Female
 - \sqcap \forall has-child.(Doctor \sqcup Lawyer)

DL Syntax and Semantics

Semantics given by interpretation $\mathcal{I} = (\Delta^{\mathcal{I}}, \cdot^{\mathcal{I}})$

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Constructor	Syntax	Example	Semantics	
atomic concept	A	Human	$A^{\mathcal{I}} \subseteq \Delta^{\mathcal{I}}$	
atomic role	R	has-child	$R^{\mathcal{I}} \subseteq \Delta^{\mathcal{I}} \times \Delta^{\mathcal{I}}$	
and for C , D concepts and R a role name				
conjunction	$C\sqcap D$	Human ⊓ Male	$C^{\mathcal{I}} \cap D^{\mathcal{I}}$	
disjunction	$C \sqcup D$	Doctor ⊔ Lawyer	$C^{\mathcal{I}} \cup D^{\mathcal{I}}$	
negation	$\neg C$	⊣Male	$\Delta^{\mathcal{I}} \setminus C$	
exists restr.	$\exists R.C$	∃has-child.Male	$\{x \mid \exists y. \langle x, y \rangle \in R^{\mathcal{I}} \land y \in C^{\mathcal{I}}\}$	
value restr.	$\forall R.C$	∀has-child.Doctor	$\{x \mid \forall y. \langle x, y \rangle \in R^{\mathcal{I}} \implies y \in C^{\mathcal{I}}\}$	

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Constructor	Syntax	Example	Semantics
qualified num	$\geqslant nR.C$	\geqslant 3 child. female	$\{x \mid \{y.(\langle x, y \rangle \in R^{\mathcal{I}} \land y \in C^{\mathcal{I}})\} \ge n\}$
restrictions	$\leqslant nR.C$	$\leqslant 1$ parent female	$\{x \mid \{y.(\langle x, y \rangle \in R^{\mathcal{I}} \land y \in C^{\mathcal{I}})\} \leqslant n\}$
inverse role	R^{-}	has-child	$\{\langle x,y\rangle\mid \langle y,x\rangle\in R^{\mathcal{I}}\}$
trans role	$^{(+)}R$	⁽⁺⁾ has-ancestor	$R^{\mathcal{I}} = (R^{\mathcal{I}})^+$

\mathcal{SHIQ}

nominals $\{x\}$ $\{\text{Italy}\}$ $\{x^{\mathcal{I}}\}$ conc. domain $f_1, \ldots, f_n.P$ earns spends <</td> $\{x \mid P(f_1^{\mathcal{I}}, \ldots, f_n^{\mathcal{I}})\}$

 $\mathcal{SHOIQ}(D_n)$

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 $A \doteq C, A \sqsubseteq C$ Father \doteq Man $\sqcap \exists$ has-child.Human Human \sqsubseteq Animal \sqcap Biped

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 $A \doteq C, A \sqsubseteq C$ Father \doteq Man $\sqcap \exists$ has-child.Human Human \sqsubseteq Animal \sqcap Biped Inclusion (GCI) axioms assert subsumption relations $C \sqsubseteq D$ (note $C \doteq D$ equivalent to $C \sqsubseteq D$ and $D \sqsubseteq C$) \exists has-degree.Masters $\sqsubseteq \exists$ has-degree.Bachelors

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An interpretation \mathcal{I} satisfies

 $C \doteq D \quad \text{iff} \quad C^{\mathcal{I}} = D^{\mathcal{I}} \qquad C \sqsubseteq D \quad \text{iff} \quad C^{\mathcal{I}} \subseteq D^{\mathcal{I}}$

A **Tbox** T iff it satisfies every axiom in T ($T \models T$)

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An interpretation $\mathcal I$ satisfies

 $\begin{aligned} a: C & \text{iff} \quad a^{\mathcal{I}} \in C^{\mathcal{I}} \quad \langle a, b \rangle : R & \text{iff} \quad \langle a^{\mathcal{I}}, b^{\mathcal{I}} \rangle \in R^{\mathcal{I}} \\ \text{An Abox } \mathcal{A} & \text{iff it satisfies every axiom in } \mathcal{A} (\mathcal{I} \models \mathcal{A}) \\ \text{A KB } \Sigma = \langle \mathcal{T}, \mathcal{A} \rangle & \text{iff it satisfies both } \mathcal{T} & \text{and } \mathcal{A} (\mathcal{I} \models \Sigma) \end{aligned}$

Why Tbox and Abox?

- Restricted use of individuals maintains (kind of) tree model property
 - Arbitrary but finite directed graph connecting named individuals
 - Named individuals roots of (possibly) infinite trees of anonymous individuals
 - Lower complexity class (ExpTime for *SHIQ*)
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- Note that with nominals, Abox becomes syntactic sugar
 - a: C equiv. to $\{a\} \sqsubseteq C$
 - $\langle a, b \rangle : R$ equiv. to $\{a\} \sqsubseteq \exists R.\{b\}$

Subsumption (structure knowledge, compute taxonomy) $C \sqsubseteq D$? Is $C^{\mathcal{I}} \subseteq D^{\mathcal{I}}$ in all interpretations? Subsumption (structure knowledge, compute taxonomy) $C \sqsubseteq D$? Is $C^{\mathcal{I}} \subseteq D^{\mathcal{I}}$ in all interpretations?

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Problems are **closely related**:

 $\begin{array}{lll} C \sqsubseteq_{\mathcal{T}} D & \text{iff} & C \sqcap \neg D \text{ is inconsistent w.r.t. } \mathcal{T} \\ C \text{ is consistent w.r.t. } \mathcal{T} & \text{iff} & C \not\sqsubseteq_{\mathcal{T}} A \sqcap \neg A \end{array}$

Reasoning Techniques

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- Blocking ensures termination (with expressive DLs)















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 - Inverse roles
 - Concrete domains
 - Aboxes
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- Extend expansion rules and use more sophisticated blocking strategy
- Forest instead of Tree (for Aboxes)

Implementing DL Systems


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 - Mitigated by:
 - → Careful choice of algorithm
 - Highly optimised implementation

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 - GCI axioms can be used to "encode" additional operators/axioms

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 - BUT even simple domain encoding is disastrous with large numbers of roles

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Modern systems include MANY optimisations, e.g.:

Optimised classification

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 - Heuristic ordering of propositional and modal expansion

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 - Effect is to prune away part of the search space
- Highly effective essential for usable system
 - E.g., GALEN KB, 30s (with) \longrightarrow months++ (without)

















Axioms and Rules

Rules (at least KR rules) can be seen as a form of axiom, e.g.:

$$p(x) \leftarrow q(x) \land w(x) \equiv p \sqsubseteq q \sqcap w$$
$$p(x) \leftarrow q(x) \land r(x, y) \land w(y) \equiv p \sqsubseteq q \sqcap \exists r.w$$

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- Closed world doesn't make sense in ontologies

E.g., the "discount" example:

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\begin{array}{lll} \mathsf{discount}(x,7\%) & \leftarrow & \mathsf{customer}(x) \land \mathsf{category}(x,y) \\ & & \wedge \mathsf{premium}(y) \land \mathsf{buys}(x,z) \land \mathsf{product}(z) \\ & & \wedge \mathsf{category}(z,w) \land \mathsf{luxury}(w) \end{array}
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can be written in DL as:

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can be written in DL as:

- $\exists discount.7\% \sqsubseteq customer \sqcap \exists category.premium \\ \sqcap \exists buys.(product \sqcap \exists category.luxury)$
- May not capture intended semantics
 - Should be able to fix this by modeling transactions instead of customers

Query Rules

Query rules have a completely different semantics

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says answer = $\{x | KB \models \exists y(q(x) \land r(x, y))\}$

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Applications can implement many "rule-like" features using queries

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Horn rules with no extensions (probably) can't capture:

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- Can't combine with expressive DLs (and still stay decidable)
 - adding these constructs to SHIQ leads to undecidability

Intersection of Rules and DLs

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 - conjunction in head (\equiv multiple rules)
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 - conjunction in head (\equiv multiple rules)
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- Result is a strange and asymmetrical DL

Other Approaches

- Can layer rules on top of DL
 - rule predicates can be DL classes or roles
 - several examples have been implemented
 - best known is Carin system from Levy & Rousset
 - undecidable unless DL is very weak (Carin uses Classic)

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- Some existing work on language fusions and hybrid reasoners

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- Nominals
- Extensions to DAML+OIL
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- New reasoning tasks
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Increased Expressive Power: Datatypes

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 - All XMLS datatypes supported
- Already seeing some (limited) implementations
 - E.g., Cerebra system (Network Inference)

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- Relatively straightforward (in theory) without inverse roles
 - Algorithm for $\mathcal{SHOQ}(\mathbf{D})$ deals with nominals
 - Practical implementation still to be demonstrated

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- How can reasoners be developed/adapted for extended languages?

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 - Web ontologies can be expected to grow very large
- Reasoning with individuals (Abox)
 - Deployment of web ontologies will mean reasoning with (possibly very large numbers of) individuals
 - Standard Abox techniques may not be able to cope



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- Problem exacerbated by over-cautious double blocking condition (e.g., root node can never block)
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Caching and merging

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- Reasoning with very large KBs
 - DL systems shown to work with ${\approx}100k$ concept KB [Haarslev & Möller]
 - But KB only exploited small part of DL language

Tools and infrastructure required in order support use of DAML+OIL
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 - Several editors available, e.g, OilEd (Manchester), OntoEdit (Karlsruhe), Protégé (Stanford)

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- DLs are logic based KR formalisms with emphasis on reasoning
- DL systems provide efficient reasoning services
 - Careful choice of logic/algorithm
 - Highly optimised implementation

Resources

Slides from this talk

```
www.cs.man.ac.uk/~horrocks/Slides/dagstuhl070202.pdf
```

FaCT system

```
www.cs.man.ac.uk/fact
```

OIL

```
www.ontoknowledge.org/oil/
```

DAML+OIL

www.daml.org/language/

OilEd

img.cs.man.ac.uk/oil

I.COM

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