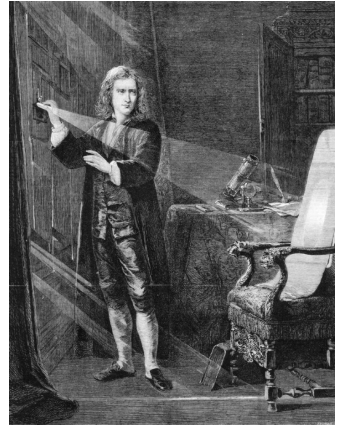
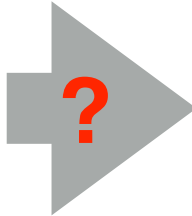
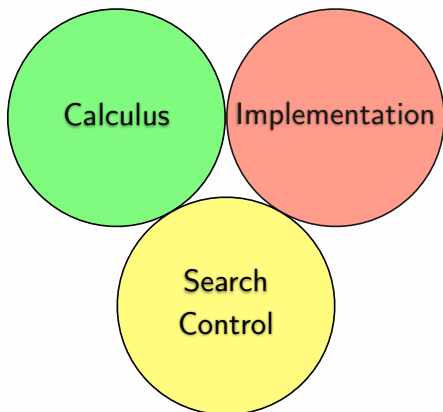


# We know (nearly) nothing!

But can we learn?



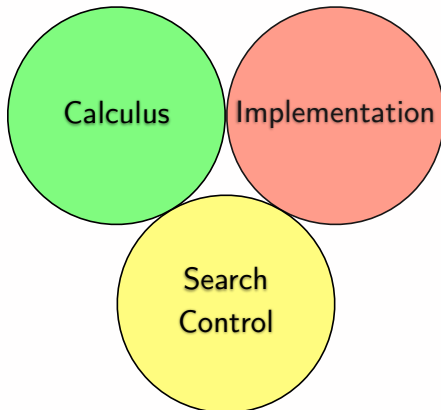
# Driving the State of the Art



# Driving the State of the Art

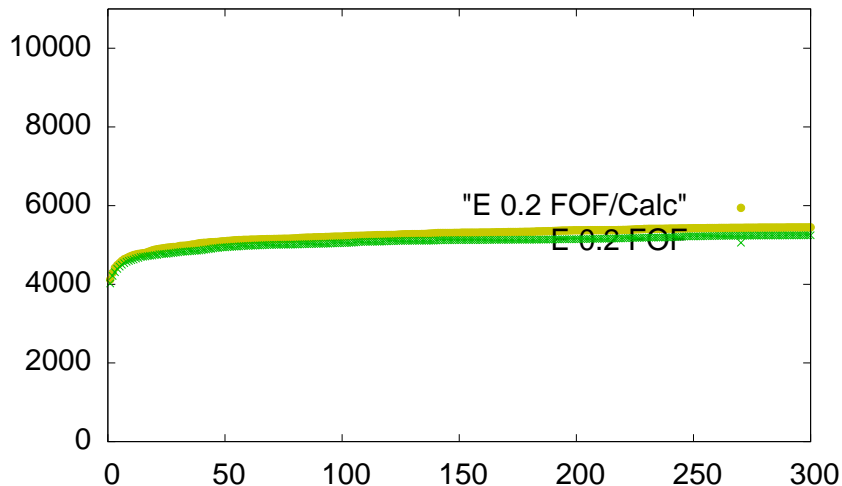
**What** inference system to use?

**How** to do inferences efficiently?

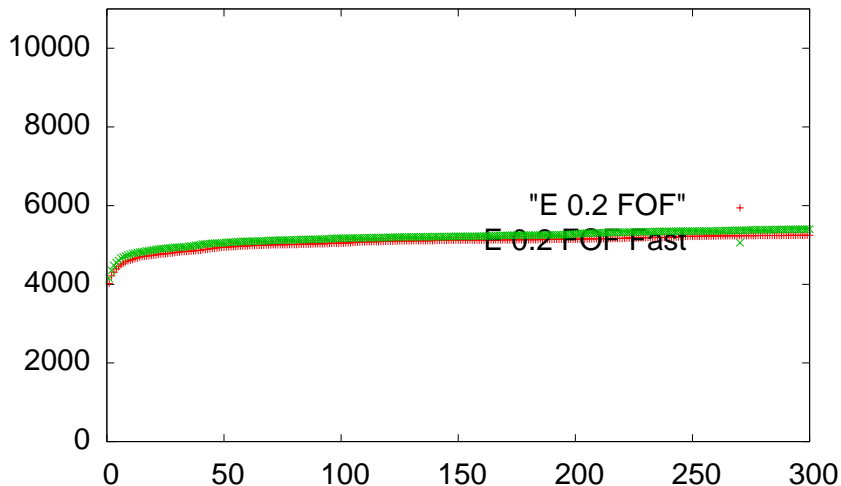


**Where** to search for proofs?

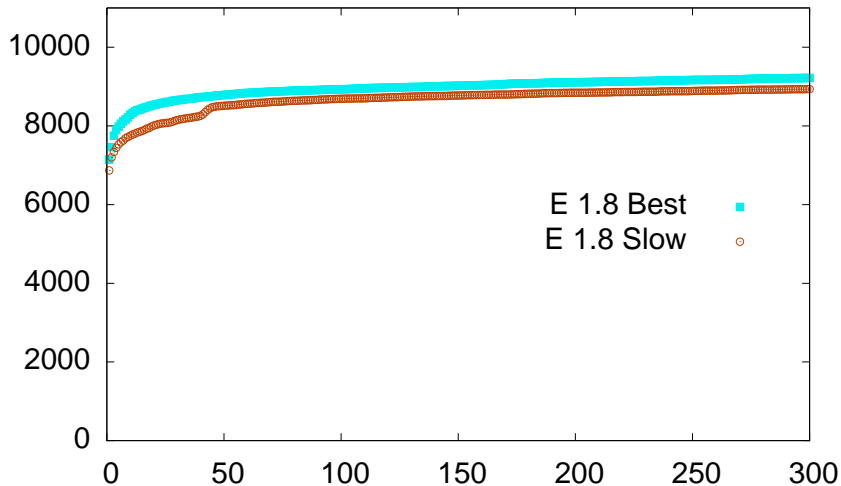
# Evolution of Calculus



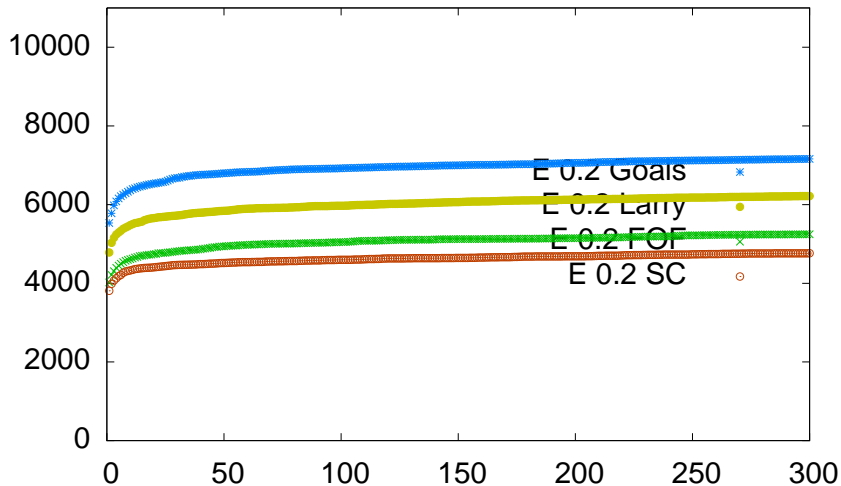
# Evolution of Implementation



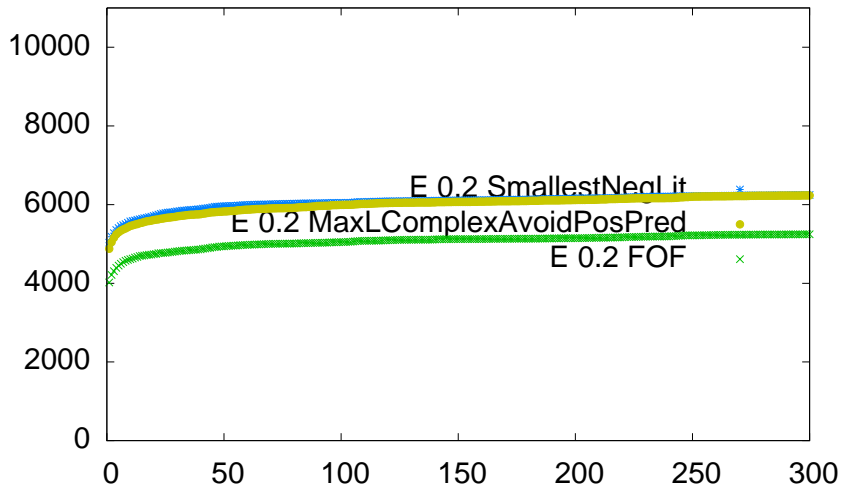
# Evolution of Implementation



# Evolution of Search Control/Clause Selection

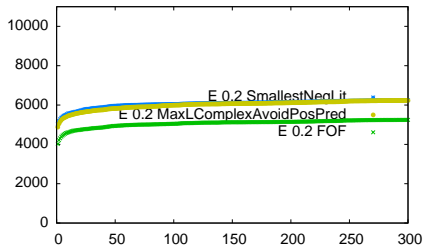
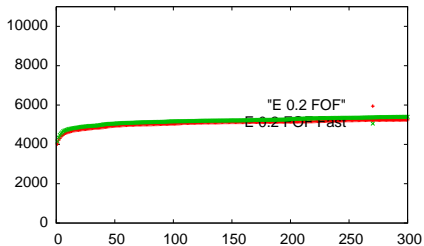
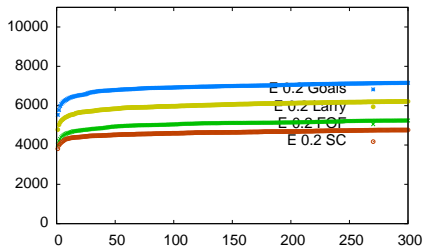
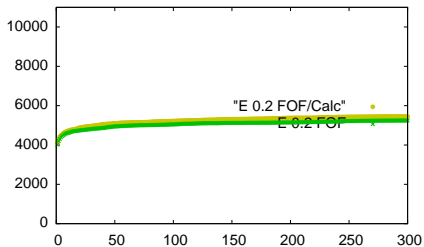


# Evolution of Search Control/Literal Selection



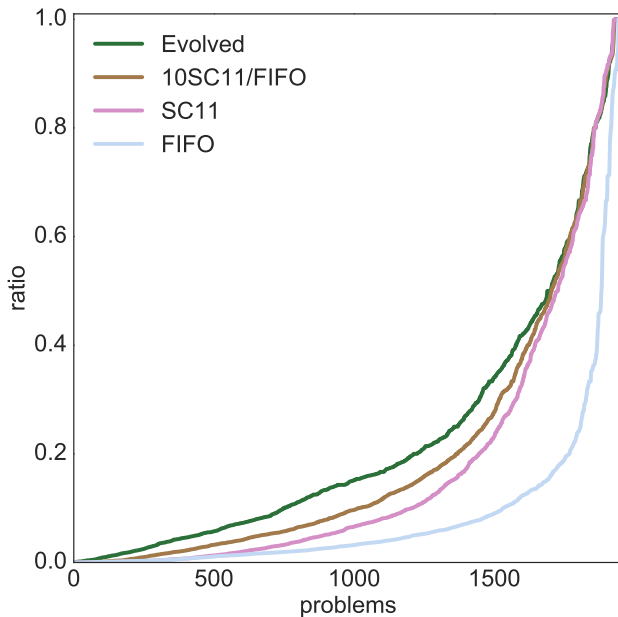


# Compare and Contrast



**Improving heuristics has been the main source  
of progress in proof search!**

... and our heuristics still suck!



# Humans are Inadequate!

- ▶ We are not good at keeping large amounts of data in our head
- ▶ We are not good at analysing large amounts of data without help
- ▶ We are not good visualising complex relationships

**Compare “The Magical Number Seven, Plus or Minus Two”**

# Player of Games

## ▶ Chess

- ▶ State: Different pieces on an 8x8 board
- ▶ Choice point: Which piece moves where
  - ▶ (Opening)
- ▶ Success: Capture of the king



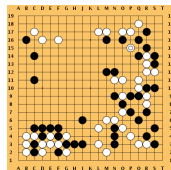
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## ▶ Go

- ▶ State: Configuration of stones on a 19x19 board
- ▶ Choice point: Where to place the next stone
- ▶ Success: Control of larger area of the board



# Player of Games

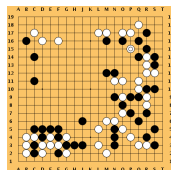
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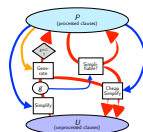
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## ▶ Saturating theorem proving

- ▶ State: Set of clauses
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  - ▶ Pick term ordering, literal selection strategy
- ▶ Success: Derivation of the empty clause



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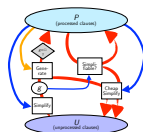
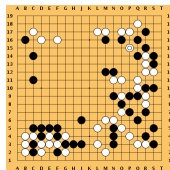
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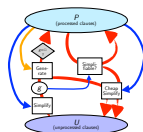
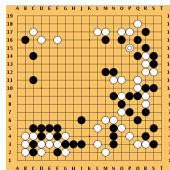
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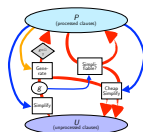
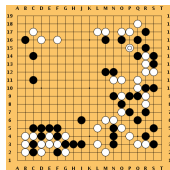
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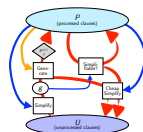
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# Grand Challenge



**Integrate Machine Learning and Symbolic Reasoning**

- ▶ Should we target domain-specific or more general search control knowledge?
- ▶ Deep learning or hand-selected features - which is better for learning search control knowledge?
- ▶ What is a better source for learning: Meta-information (success/failure, time to success, . . . ), full proofs, or even full search protocols?

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**Discuss away!**