

Boosting for Probability Estimation & Cost-Sensitive Learning

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Engineering and Physical Sciences
Research Council



The University of Manchester

Introduction:
Supervised Machine Learning Basics
(Classification)

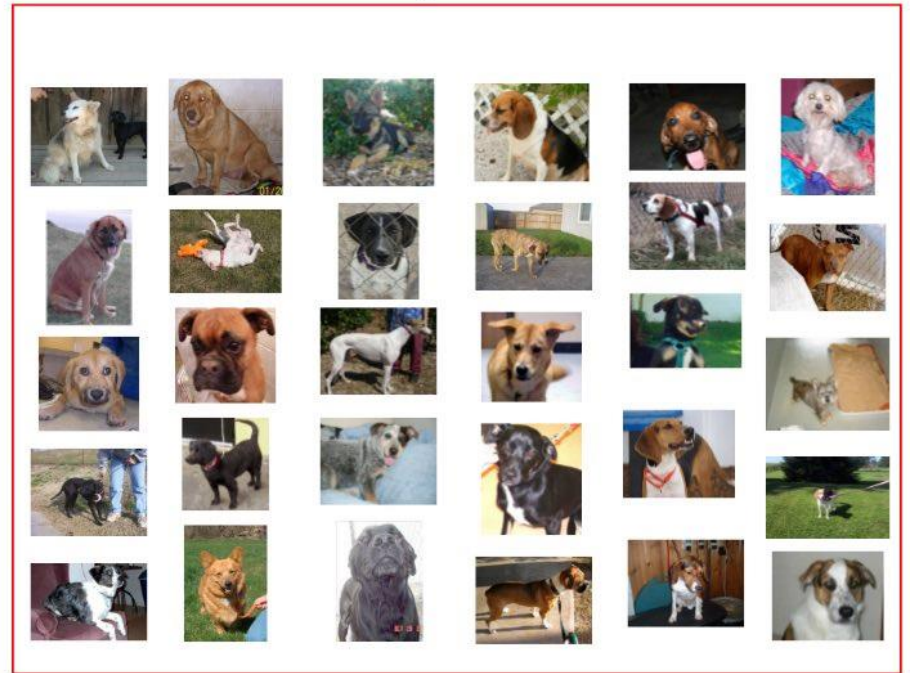
Classification

Example: Cat vs. Dog classifier

Cats



Dogs



Machine learning basics: training

TRAINING DATA

Features
(e.g. RGB value
of each pixel)

Examples
(Images)



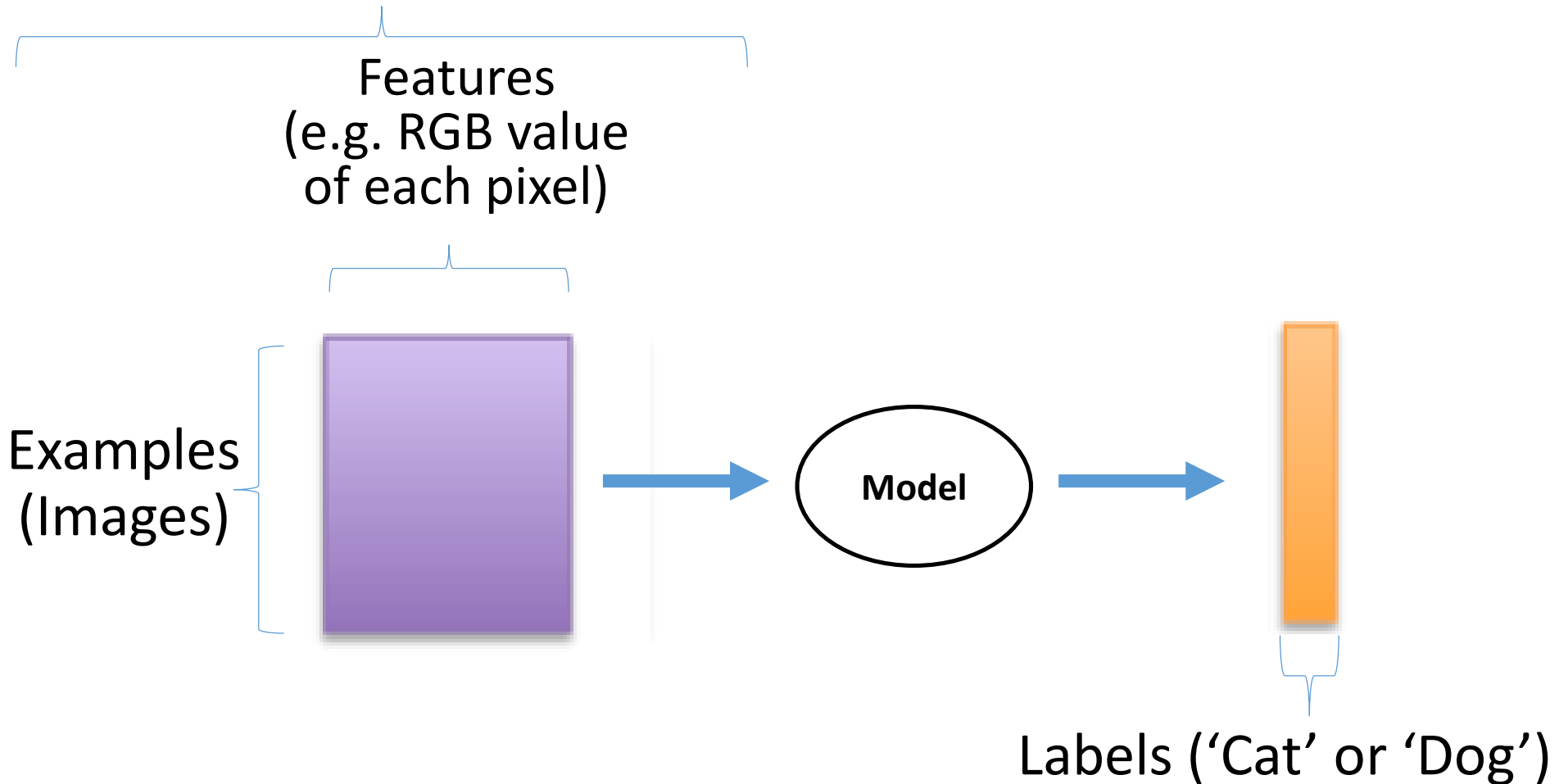
LEARNING
ALGORITHM

Model

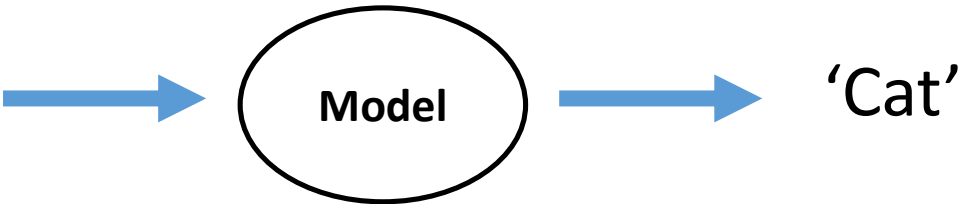
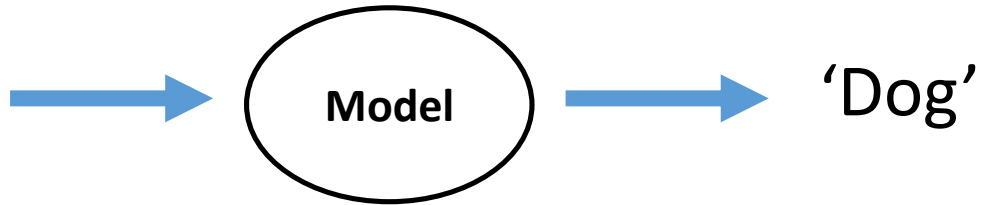
Labels ('Cat' or 'Dog')

Machine learning basics: prediction

TEST DATA

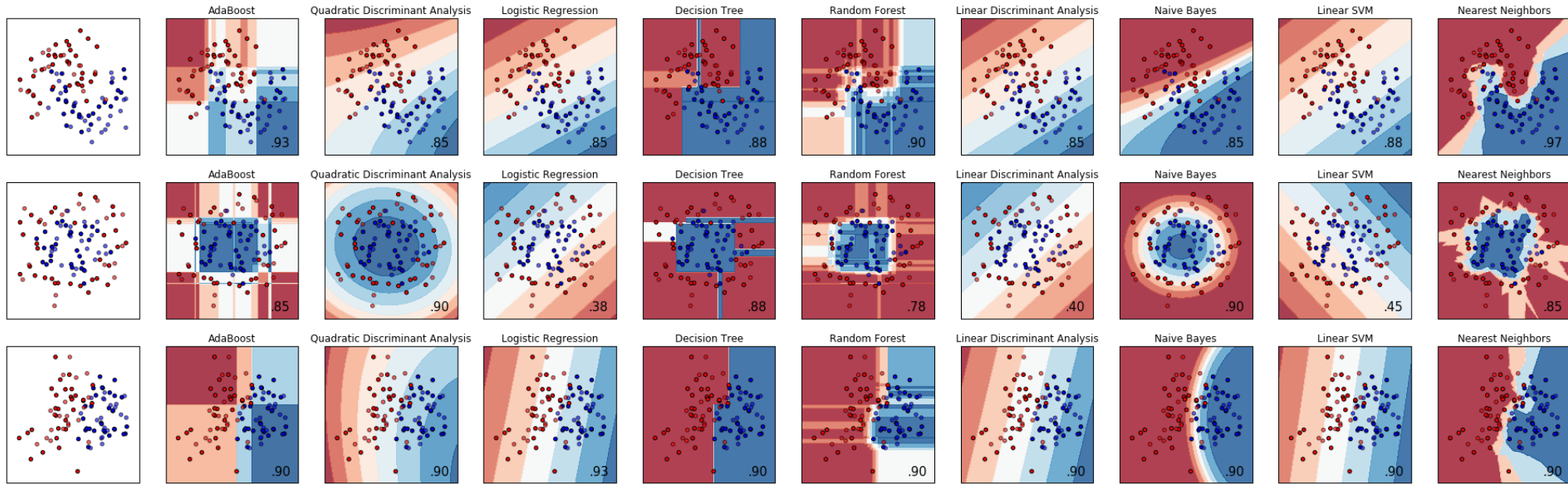


Machine learning basics: prediction



The learning algorithm's job

Given a set of points in some space belonging to different classes...

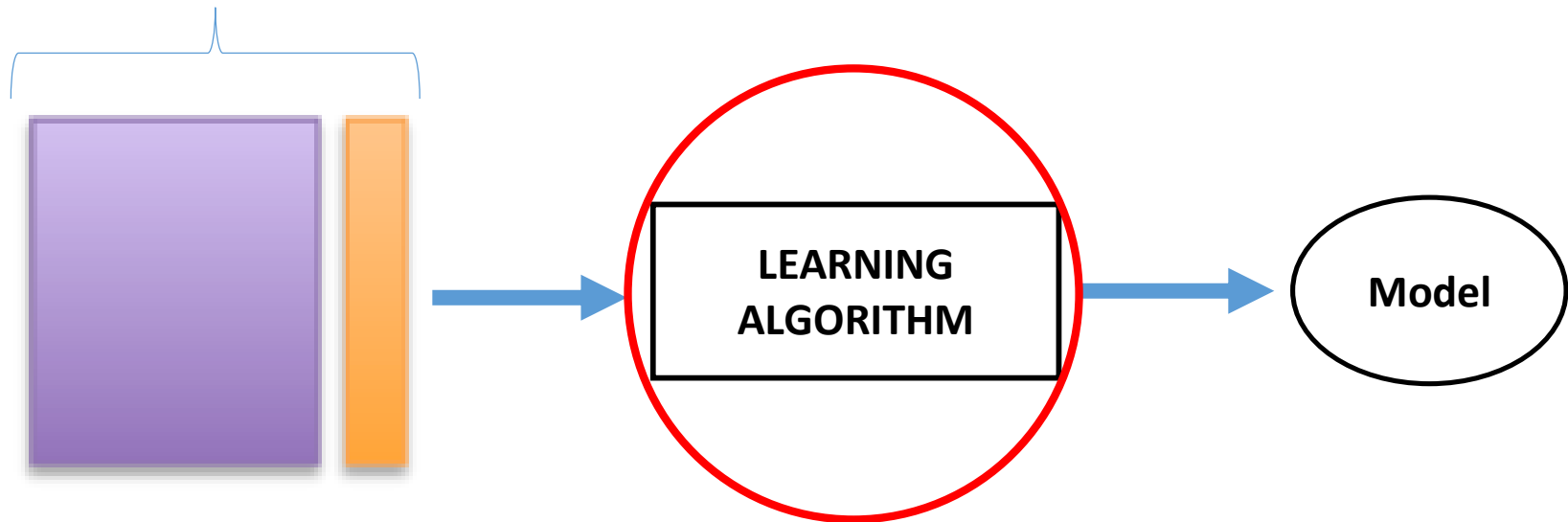


Learn a **decision surface** that **'best' separates classes**

Many **learning algorithms** each with its own **assumptions** (statistical, probabilistic, mathematical, geometrical, ...)

In this talk...

TRAINING DATA



We focus on **BOOSTING**, a specific family of **learning algorithms**
Meta-learning algorithms - can **apply to other learning algorithms** improving their performance

More specifically...

BOOSTING in **cost-sensitive** scenarios



		Actual Value	
		positives	negatives
Predicted Value	positives	TP True Positive	FP False Positive
	negatives	FN False Negative	TN True Negative

cost of a FP \neq cost of a FN

Part I:
What is wrong with
cost-sensitive Boosting?

Boosting

Can we turn a **weak learner** into a **strong learner**? (Kearns, 1988)

Marginally more
accurate than
random
guessing

Arbitrarily
high
accuracy



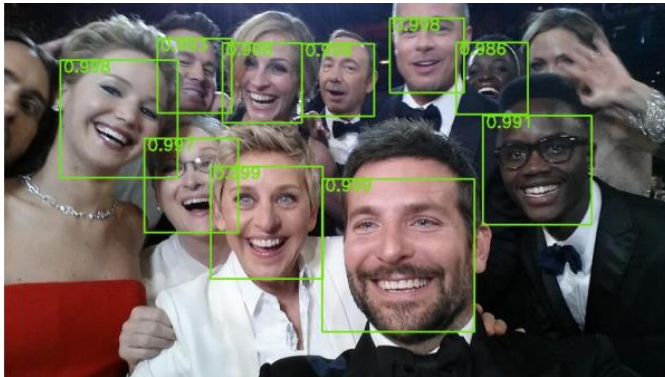
AdaBoost (Freund & Schapire, 1997)

Gradient Boosting (Friedman, 1999; Mason et al., 1999)

Gödel Prize 2003

Boosting

Very **successful** in comparisons, applications & competitions



kaggle
YAHOO!

Rich **theoretical depth**:

PAC learning, VC theory, margin theory, optimization, decision theory, game theory, probabilistic modelling, information theory, dynamical systems, ...

Adaboost (Freund & Schapire 1997)

Ensemble method.

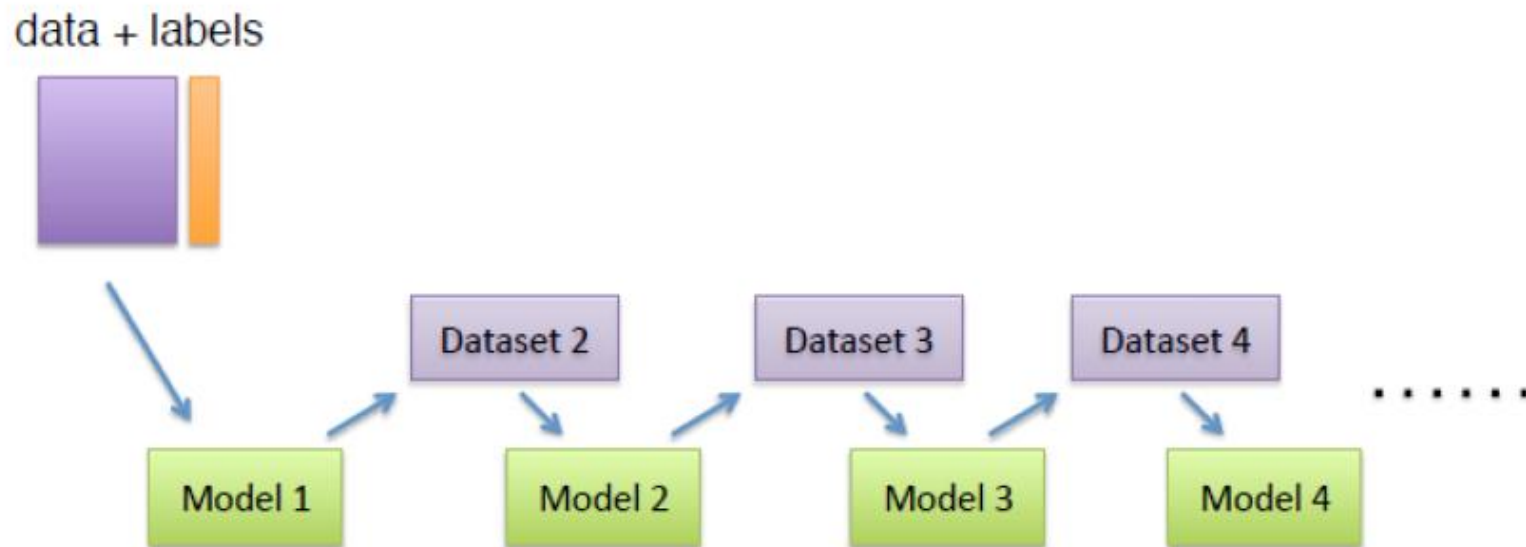
Train models **sequentially**.

Each model **focuses on examples previously misclassified**.

Combine by **weighted majority vote**.

AdaBoost: training

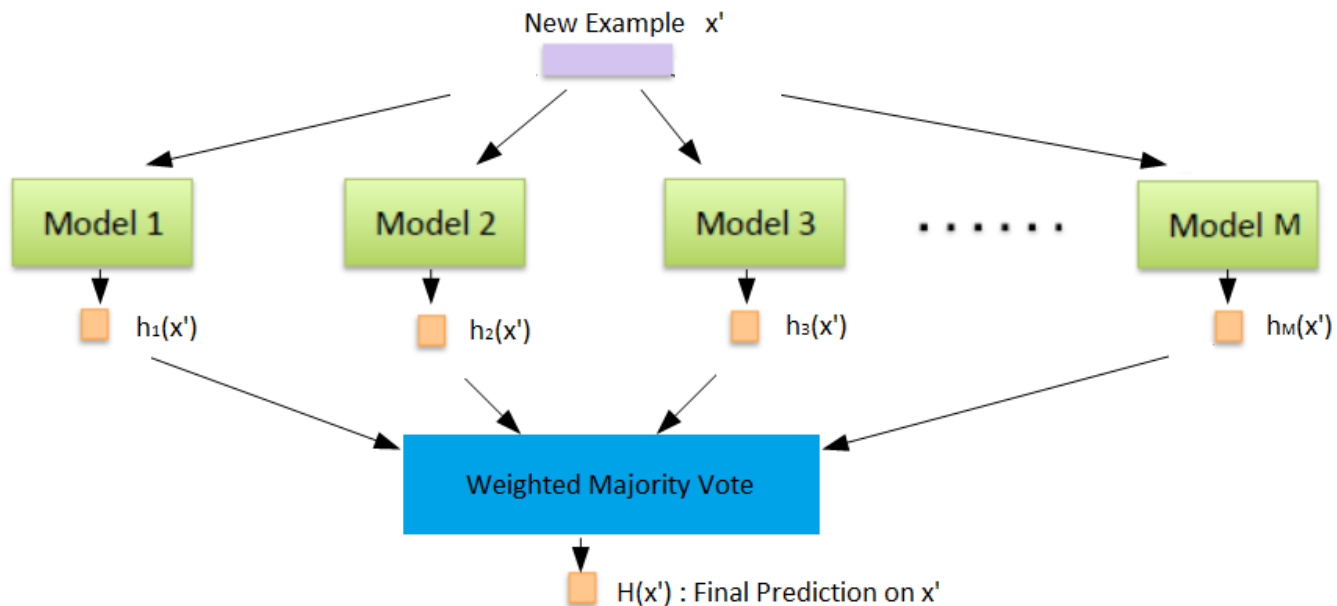
Construct strong model **sequentially** by combining multiple weak models



Each model reweights/resamples the data, emphasizing on the examples the previous one misclassified – i.e. each model focuses on **correcting the mistakes of the previous one**

AdaBoost: predictions

Prediction: **weighted majority vote** among M weak learners



AdaBoost: algorithm

Define a distribution over the training set, $D_1(i) = \frac{1}{N}, \forall i$. — **Initial weight distribution**

for $t = 1$ **to** T **do**

 Build a classifier h_t from the training set, using distribution D_t .

 Set $\alpha_t = \frac{1}{2} \ln \left(\frac{1-\epsilon_t}{\epsilon_t} \right)$ — **Majority voting confidence in classifier t**

 Update D_{t+1} from D_t :

 Set $D_{t+1}(i) = \frac{D_t(i)e^{-\alpha_t y_i h_t(x_i)}}{Z_t}$ — **Distribution update**

end for

$$H(x') = \text{sign} \left(\sum_{t=1}^T \alpha_t h_t(x') \right) \quad \text{— Majority vote on test example } x'$$

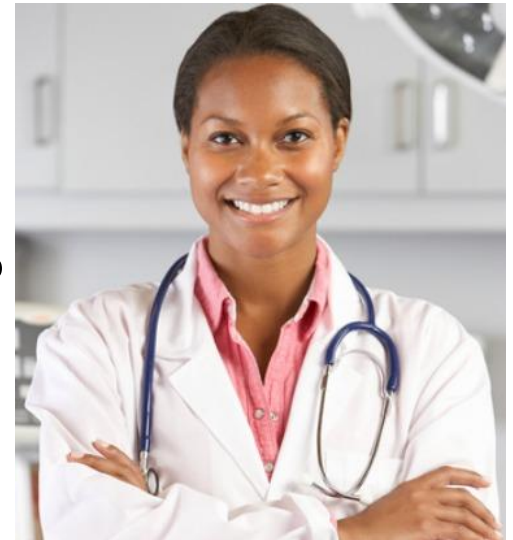
[Pos & Neg class encoded as +1 & -1 respectively for both predictions $h_t(x)$ and labels y]

Adaboost

How will it work on cost sensitive* problems? $\begin{bmatrix} 0 & c_{FN} \\ c_{FP} & 0 \end{bmatrix}$

i.e. with differing cost for a False Positive / False Negative ...

...does it **minimize** the **expected cost** (a.k.a. **risk**)?



*note: cost-sensitive & imbalanced class learning **duality**

Cost sensitive Adaboost...

AdaBoost (Freund & Schapire 1997)

AdaCost (Fan et al. 1999)

AdaCost(β_2) (Ting 2000)

CSB0 (Ting 1998)

CSB1 (Ting 2000)

CSB2 (Ting 2000)

AdaC1 (Sun et al. 2005, 2007)

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CSAda (Mashnadi-Shirazi & Vasconcelos 2007, 2011)

AdaDB (Landesa-Vázquez & Alba-Castro 2013)

AdaMEC (Ting 2000, Nikolaou & Brown 2015)

CGAda (Landesa-Vázquez & Alba-Castro 2012, 2015)

AsymAda (Viola & Jones 2002)

15+ boosting variants
over **20** years

Some **re-invented**
multiple times

Most proposed as
heuristic modifications
to original AdaBoost

Many treat FP/FN costs
as **hyperparameters**

A step back... Why is Adaboost interesting?

Functional Gradient Descent (Mason et al., 2000)

Decision Theory (Freund & Schapire, 1997)

Margin Theory (Schapire et al., 1998)

Probabilistic Modelling (Lebanon & Lafferty 2001; Edakunni et al 2011)

$$\begin{aligned} \text{Set } \alpha_t &= \frac{1}{2} \ln \left(\frac{1-\epsilon_t}{\epsilon_t} \right) \\ \text{Update } D_{t+1} &\text{ from } D_t : \\ \text{Set } D_{t+1}(i) &= \frac{D_t(i)e^{-\alpha_t y_i h_t(x_i)}}{Z_t} \end{aligned}$$

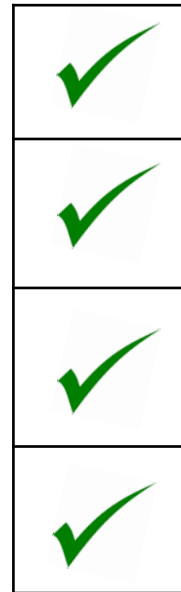
So for a cost sensitive boosting algorithm...

Functional Gradient Descent

Decision Theory

Margin Theory

Probabilistic Modelling



“Does the algorithm follow from each?”

$$\text{Set } \alpha_t = \frac{1}{2} \ln \left(\frac{1-\epsilon_t}{\epsilon_t} \right)$$

Update D_{t+1} from D_t :

$$\text{Set } D_{t+1}(i) = \frac{D_t(i)e^{-\alpha_t y_i h_t(x_i)}}{Z_t}$$

Functional Gradient Descent

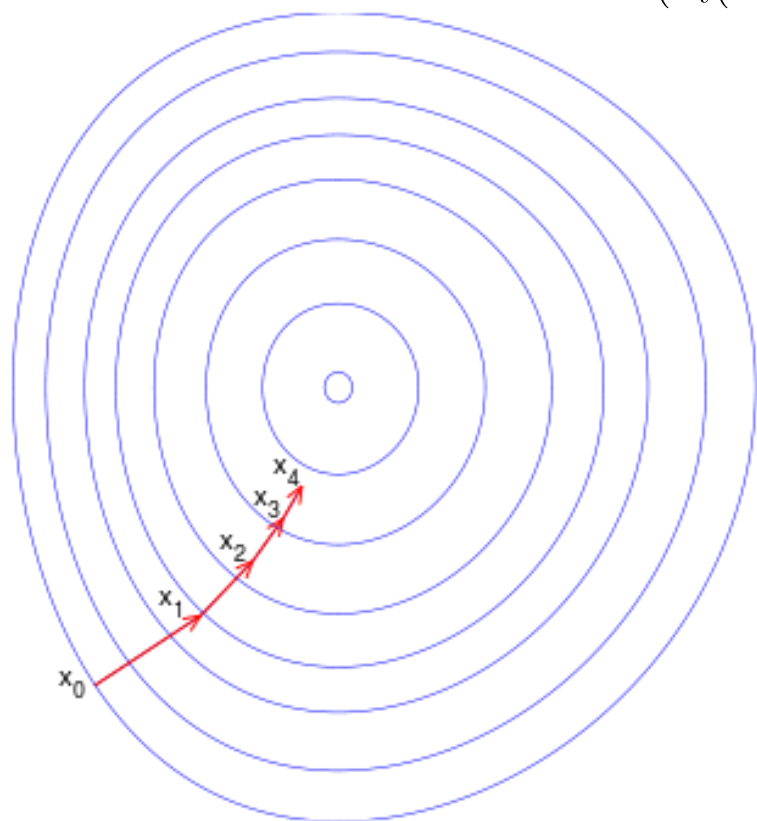
$$J(F_t(\mathbf{x})) = \frac{1}{N} \sum_{i=1}^N L(y_i F_t(\mathbf{x}_i)),$$

Direction in function space

$$D_i^{t+1} = \frac{\frac{\partial}{\partial y_i F_t(\mathbf{x}_i)} J(F_t(\mathbf{x}))}{\sum_{j=1}^N \frac{\partial}{\partial y_j F_t(\mathbf{x}_j)} J(F_t(\mathbf{x}))}$$

Step size

$$\alpha_t^* = \arg \min_{\alpha_t} \left[\frac{1}{N} \sum_{i=1}^N L(y_i (F_{t-1}(\mathbf{x}_i) + \alpha_t h_t(\mathbf{x}_i))) \right].$$



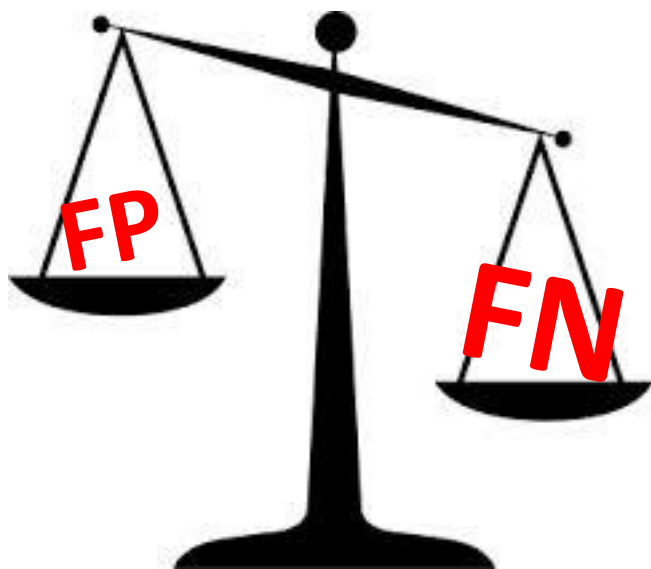
Property: FGD-consistency

Are the voting weights and distribution updates consistent with each other?

(i.e. both derivable by FGD on a given loss)

Decision theory

Ideally: Assign each example to **risk-minimizing** class:



$$\begin{bmatrix} 0 & c_{FN} \\ c_{FP} & 0 \end{bmatrix}$$

Predict class $y = 1$ iff

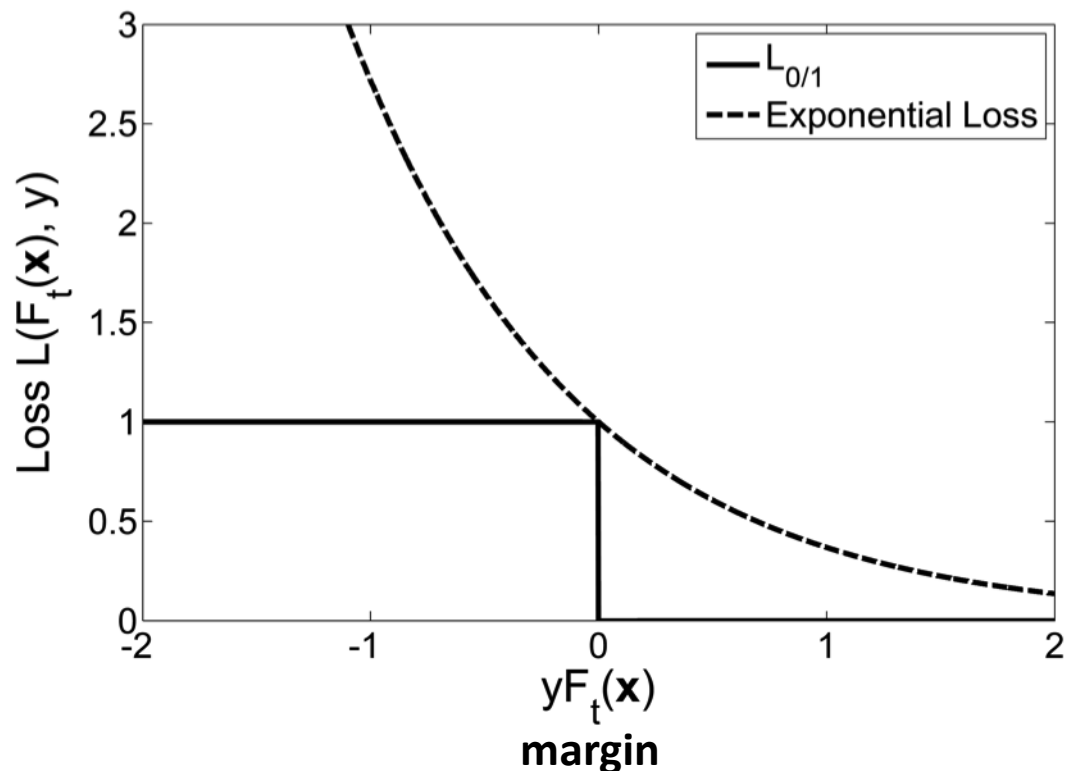
$$\hat{p}(y = 1|\mathbf{x}) > \frac{c_{FP}}{c_{FP} + c_{FN}}$$

Property: Cost-consistency

Does the algorithm use the above
(Bayes Decision Rule)
to make decisions?

(assuming 'good' probability estimates)

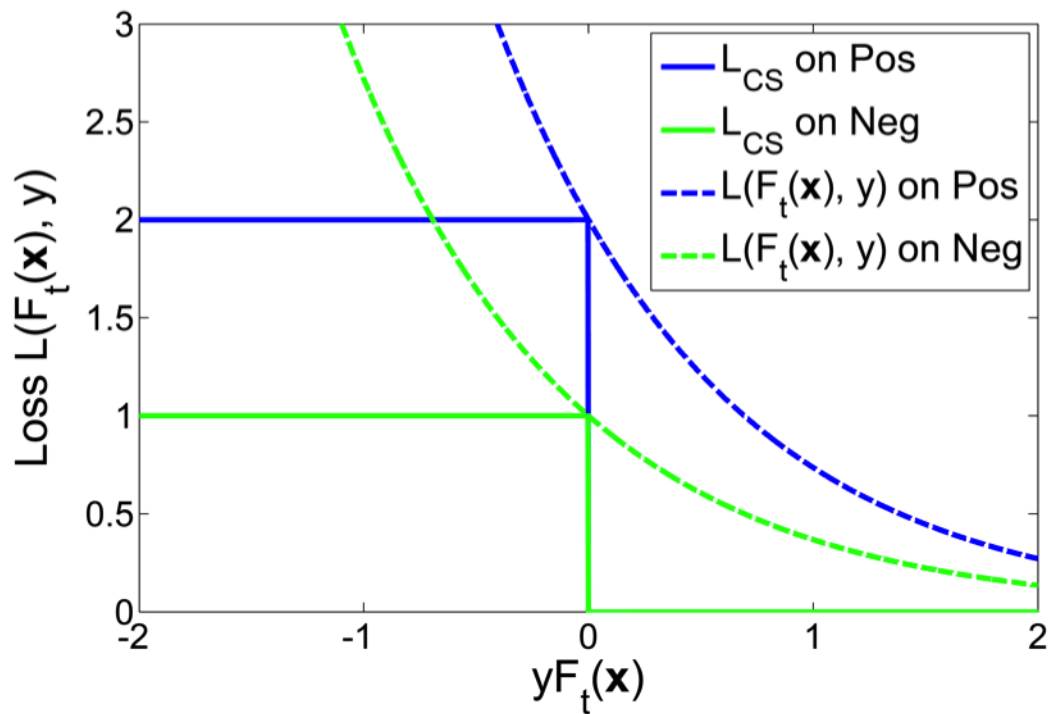
Margin theory



Sign of margin:
encodes correct (>0)
or incorrect (<0)
classification of (\mathbf{x}, y)
Magnitude of margin:
encodes confidence
of boosting ensemble
in its prediction

Large margins encourage small **generalization error**.
Adaboost promotes **large margins**.

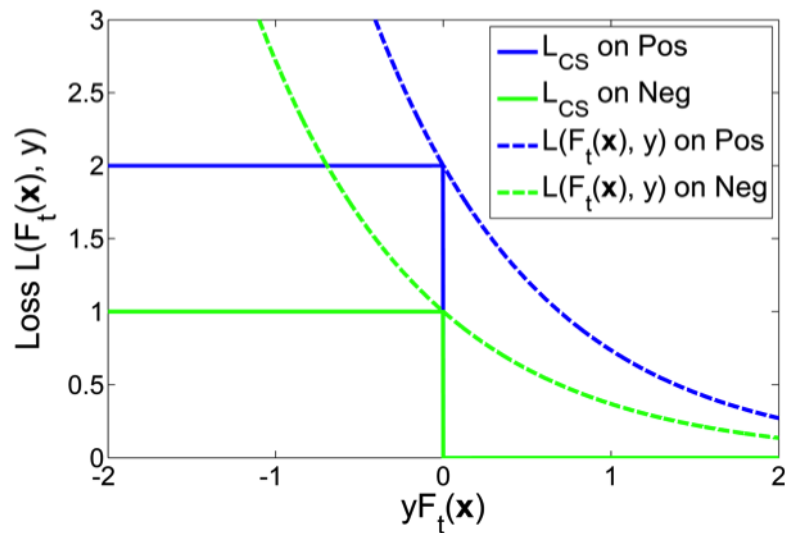
Margin theory – with costs...



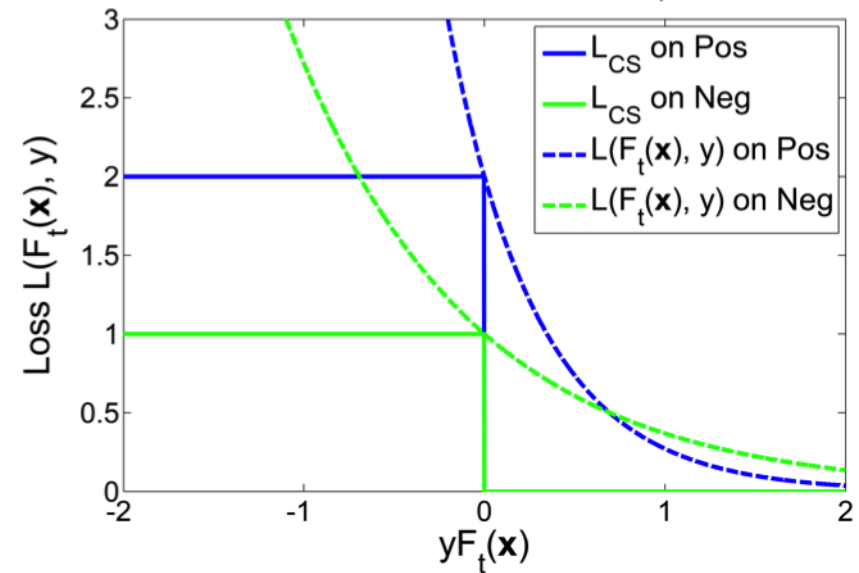
Different surrogate losses for each class.

So for a cost sensitive boosting algorithm...

We expect this to be the case.



But some algorithms do this...



Property: Asymmetry preservation

Does the loss function preserve the **relative** importance of each class, for all margin values?

Probabilistic models

‘AdaBoost does not produce good probability estimates.’

Niculescu-Mizil & Caruana, 2005

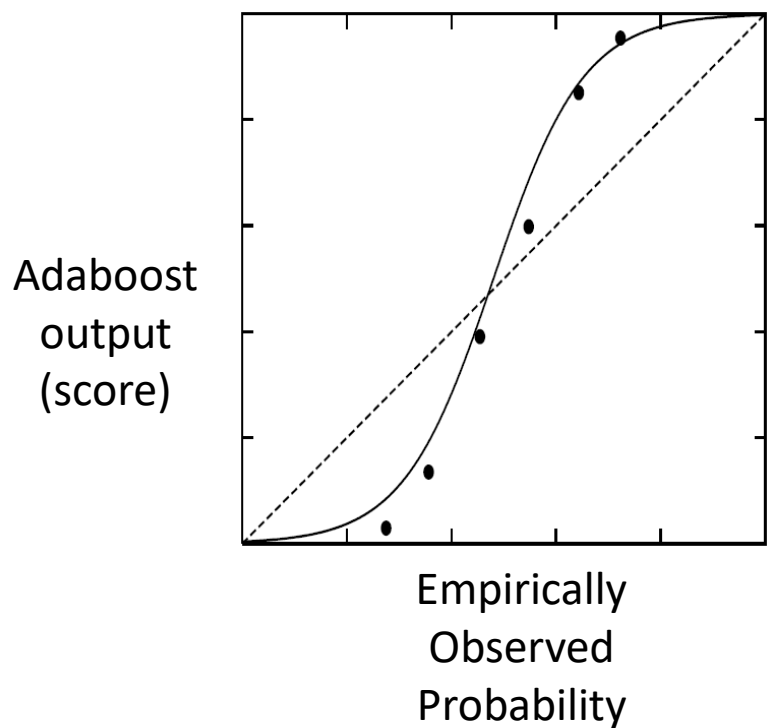
‘AdaBoost is successful at [..] classification [..] but not class probabilities.’

Mease et al., 2007

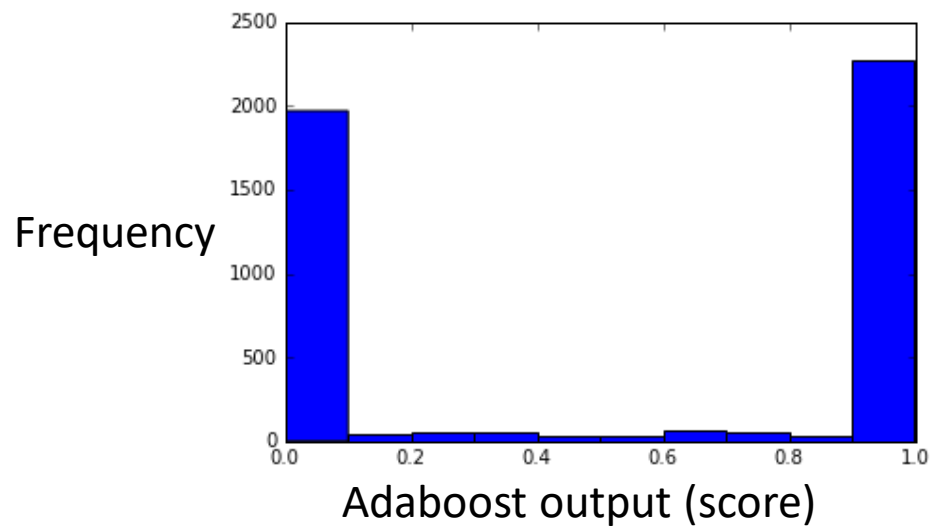
‘This increasing tendency of [the margin] impacts the probability estimates by causing them to quickly diverge to 0 and 1.’

Mease & Wyner, 2008

Probabilistic models



Adaboost tends to produce probability estimates **close to 0 or 1**.



Why this distortion?

Estimates of form:

$$\hat{p}(y = 1 | \mathbf{x}) = \frac{\sum_{\tau: h_{\tau}(\mathbf{x})=1} \alpha_{\tau}}{\sum_{\tau=1}^t \alpha_{\tau}}$$

(Niculescu-Mizil & Caruana, 2005)

As **margin** is **maximized** on training set, scores will tend to 0 or 1.

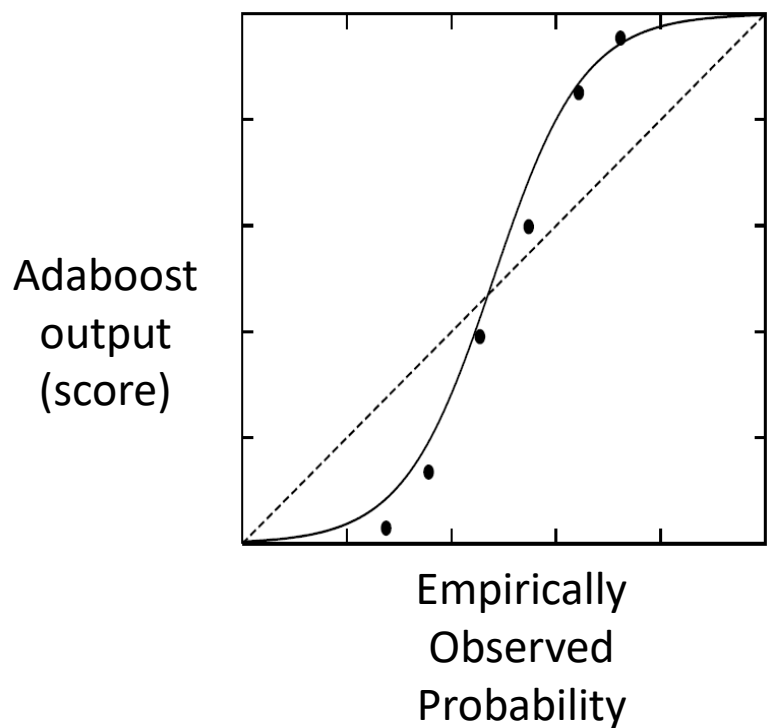
Estimates of form:

$$\hat{p}(y = 1 | \mathbf{x}) = \frac{1}{1 + e^{-2F_t(\mathbf{x})}}$$

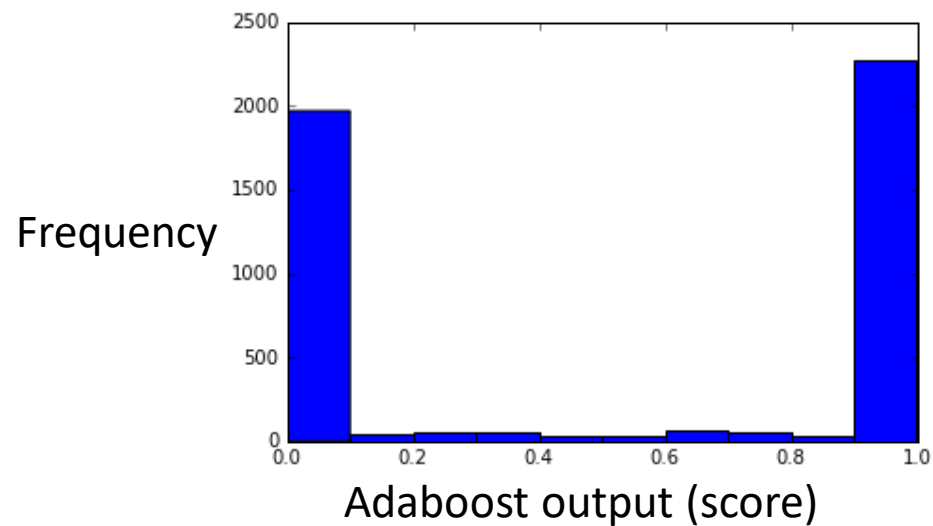
(Friedman, Hastie & Tibshirani, 2000)

Product of Experts; if one term close to 0 or 1, it dominates.

Probabilistic Models



Adaboost tends to produce probability estimates close to 0 or 1.



Property: Calibrated estimates

Does the algorithm generate “calibrated” probability estimates?

Does a given algorithm satisfy...

Property: FGD-consistency

Are the **steps consistent** with each other?

(i.e. both voting weights and distribution updates derivable by FGD on same loss)

Property: Cost-consistency

Does the algorithm use the **(risk-minimizing) Bayes Decision Rule** to make decisions?

(assuming 'good' probability estimates)

Property: Asymmetry preservation

Does the loss function **preserve the relative importance of each class**, for all margin values?

Property: Calibrated estimates

Does the algorithm generate **"calibrated" probability estimates**?

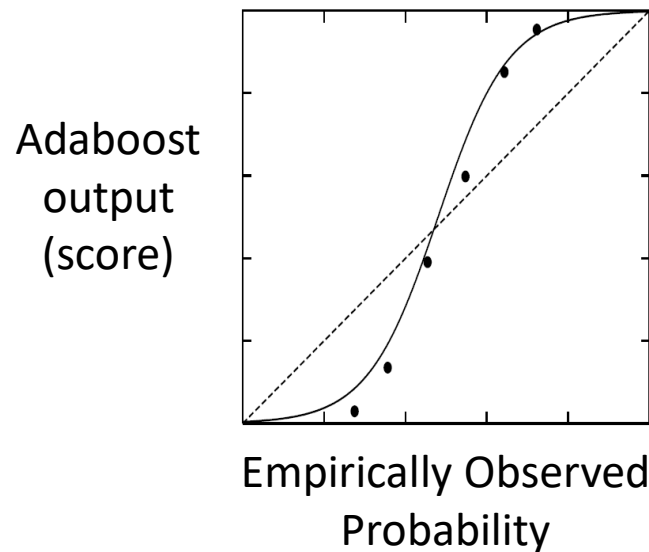
The results are in...

Method	FGD-consistent	Cost-consistent	Asymmetry-preserving	Calibrated estimates
AdaBoost (Freund & Schapire 1997)	✓		✓	<p style="text-align: center;">All algorithms produce uncalibrated probability estimates!</p>
AdaCost (Fan et al. 1999)				
AdaCost(β_2) (Ting 2000)				
CSB0 (Ting 1998)			✓	
CSB1 (Ting 2000)			✓	
CSB2 (Ting 2000)			✓	
AdaC1 (Sun et al. 2005, 2007)		✓		
AdaC2 (Sun et al. 2005, 2007)	✓		✓	
AdaC3 (Sun et al. 2005, 2007)				
CSAda (Mashnadi-Shirazi & Vasconcelos 2007, 2011)	✓	✓		
AdaDB (Landesa-Vázquez & Alba-Castro 2013)	✓	✓		
AdaMEC (Ting 2000, Nikolaou & Brown 2015)	✓	✓	✓	
CGAda (Landesa-Vázquez & Alba-Castro 2012, 2015)	✓	✓	✓	
AsymAda (Viola & Jones 2002)	✓	✓	✓	

So could we just calibrate these last three? We use “Platt scaling”.

Platt scaling (logistic calibration)

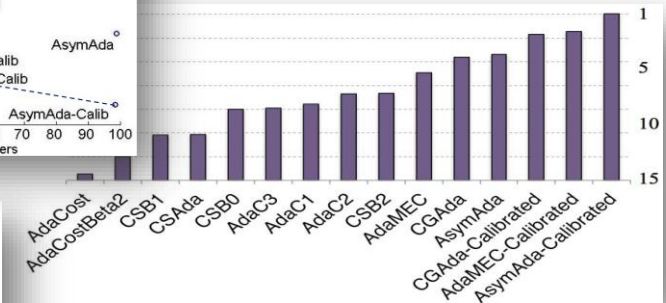
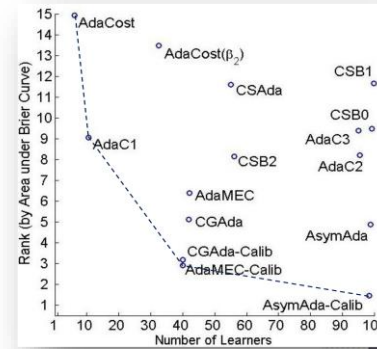
Training: Reserve part of training data (here 50% -more on this later) to **fit a sigmoid** to correct the distortion:



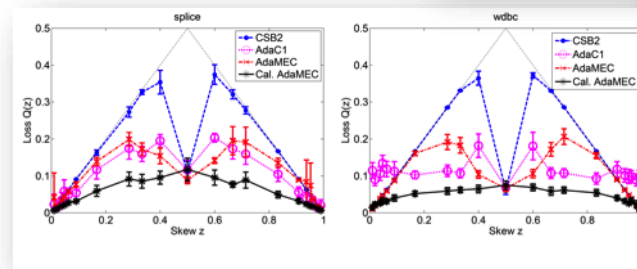
Prediction: Apply sigmoid transformation to **score** (output of ensemble) to get **probability estimate**

Experiments

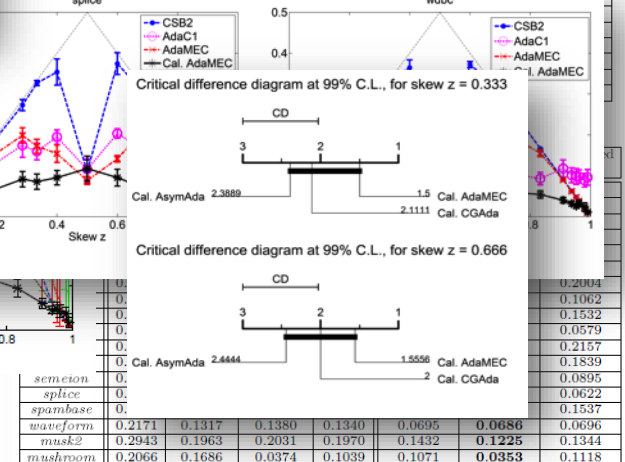
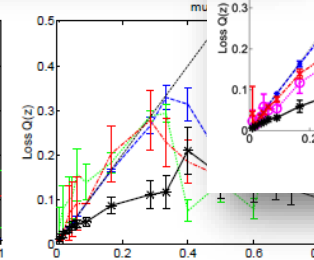
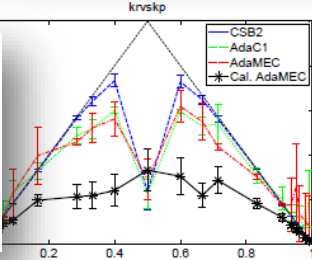
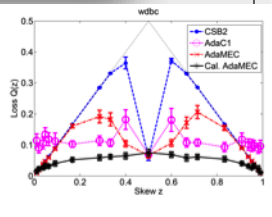
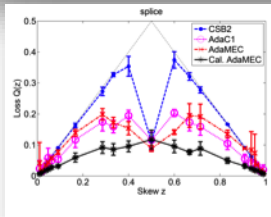
15 algorithms.
18 datasets.
21 degrees of cost imbalance.



Dataset	Calibrated AdaMEC	Calibrated AsymAda	Calibrated CGAda
survival	0.2337	0.2343	0.2328
ionosphere	0.1711	0.1994	0.1931
congress	0.0330	0.0358	0.0328
liver	0.2494	0.2622	0.2491
pima	0.2268	0.2338	0.2330
parkinsons	0.1431	0.1534	0.1474
landsat	0.2182	0.2421	0.2137
krvskp	0.0991	0.1405	0.1178
heart	0.1491	0.1522	0.1524
wdbc	0.0557	0.0626	0.0620
credit	0.2156	0.2260	0.2200
sonar	0.1828	0.1846	0.1829
semeion	0.0898	0.1341	0.1120
splice	0.0668	0.1049	0.0729
spambase	0.1421	0.2060	0.1699
waveform	0.0699	0.0688	0.0702
musk2	0.1397	0.1367	0.1408
mushroom	0.1051	0.1817	0.1281

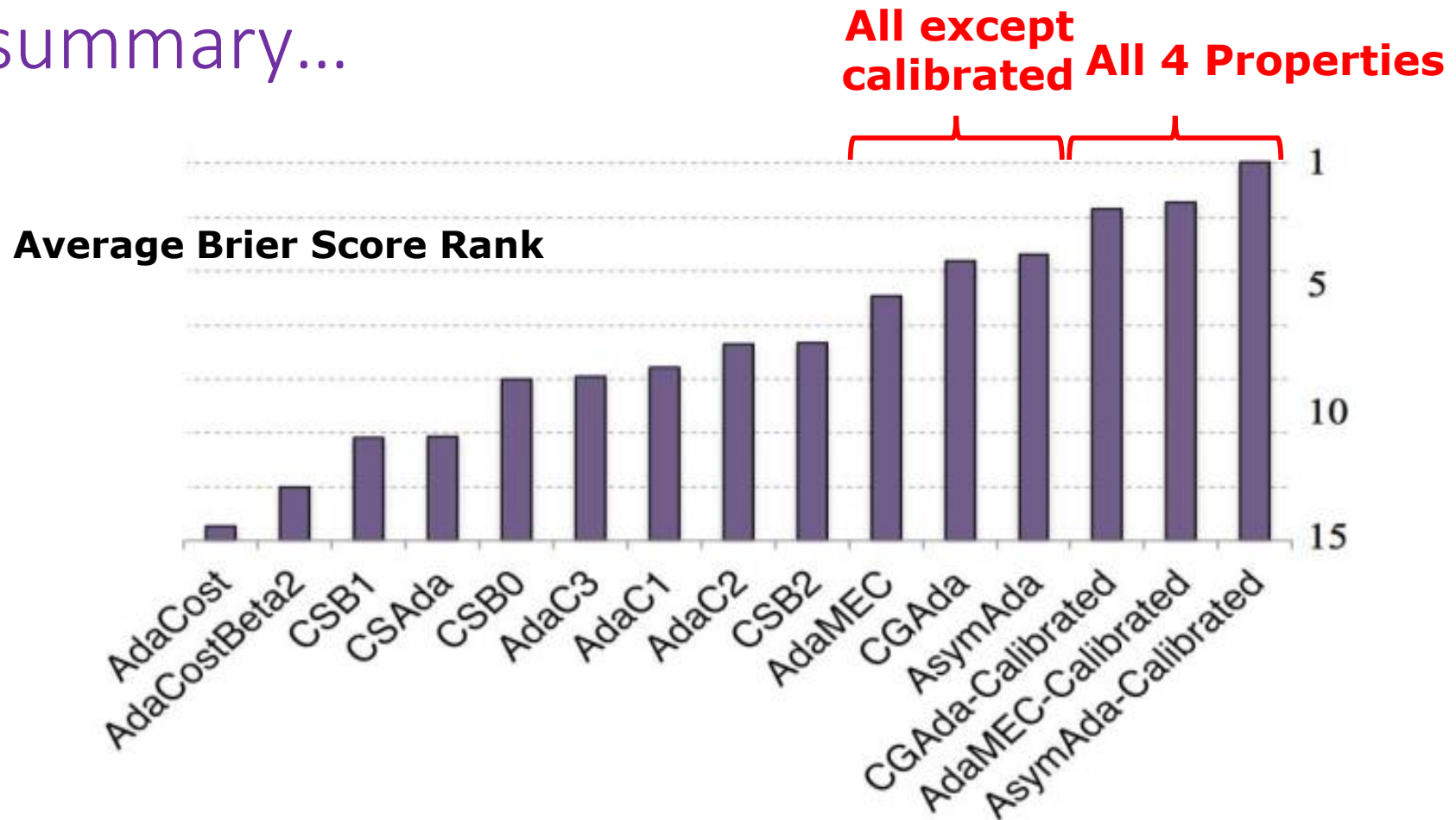


pima	0.2396	0.2512	0.2369	0.3129	0.2363	0.2370	0.4241	0.3034
parkinsons	0.2012	0.2332	0.2162	0.2359	0.2199	0.2207	0.4099	0.2799
landsat	0.2132	0.2472	0.2225	0.2131	0.2178	0.2357	0.3619	0.3079
krvskp	0.2265	0.2431	0.2036	0.1838	0.2060	0.2117	0.4175	0.2632
heart	0.2294	0.2435	0.2160	0.2887	0.2180	0.2177	0.3831	0.2836
wdbc	0.2012	0.2117	0.2002	0.1128	0.1993	0.2065	0.2696	0.2482
credit	0.2384	0.2529	0.2370	0.2766	0.2316	0.2321	0.4555	0.3064



semeion	0.	0.	0.	0.	0.	0.	0.2004	0.
splice	0.	0.	0.	0.	0.	0.	0.1062	0.
spambase	0.	0.	0.	0.	0.	0.	0.1532	0.
waveform	0.2171	0.1317	0.1380	0.1340	0.0695	0.0686	0.0696	0.
musk2	0.2943	0.1963	0.2031	0.1970	0.1432	0.1225	0.1344	0.
mushroom	0.2066	0.1686	0.0374	0.1039	0.1071	0.0353	0.1118	0.

In summary...



AdaMEC, CGAda & AsymAda **outperform all others.**

Their **calibrated** versions **outperform** the **uncalibrated** ones

In summary...

“Calibrated-AdaMEC” was one of the top methods.

1. Take original Adaboost.

2. Calibrate it (we use Platt scaling)

3. Shift the decision threshold.... : $\frac{C_{FP}}{C_{FP} + C_{FN}}$

Consistent with all theory perspectives.

No extra **hyperparameters** added.

No need to retrain if cost ratio changes.

Consistently **top (or joint top)** in empirical comparisons.

Methods & properties

Method	FGD-consistent	Cost-consistent	Asymmetry-preserving	Calibrated estimates
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CSB2 (Ting 2000)			✓	
AdaC1 (Sun et al. 2005, 2007)		✓		
AdaC2 (Sun et al. 2005, 2007)	✓		✓	
AdaC3 (Sun et al. 2005, 2007)				
CSAda (Mashnadi-Shirazi & Vasconcelos 2007, 2011)	✓	✓		
AdaDB (Landesa-Vázquez & Alba-Castro 2013)	✓	✓		
AdaMEC (Ting 2000, Nikolaou & Brown 2015)	✓	✓	✓	
CGAda (Landesa-Vázquez & Alba-Castro 2012, 2015)	✓	✓	✓	
AsymAda (Viola & Jones 2002)	✓	✓	✓	

So could we just calibrate these last three? We use “Platt scaling”.

Q: What if we calibrate all methods?

A: In **theory**, ...

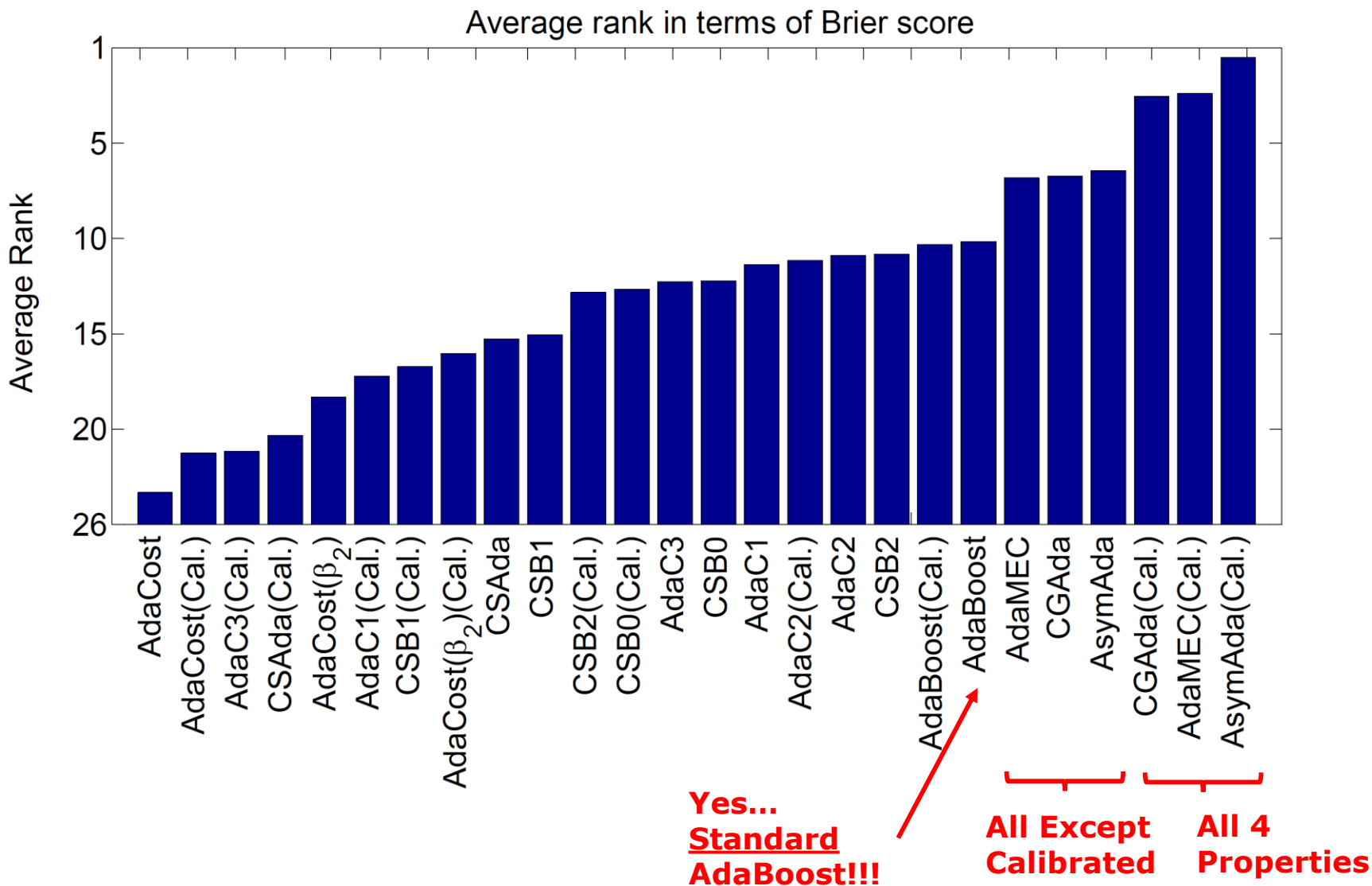
... calibration improves probability estimates.

... if a method is **not cost-sensitive**, will not make it.

... if the **steps** are **not consistent**, will not make them.

... if **class importance is swapped during training**, will not correct.

Results



Methods & properties

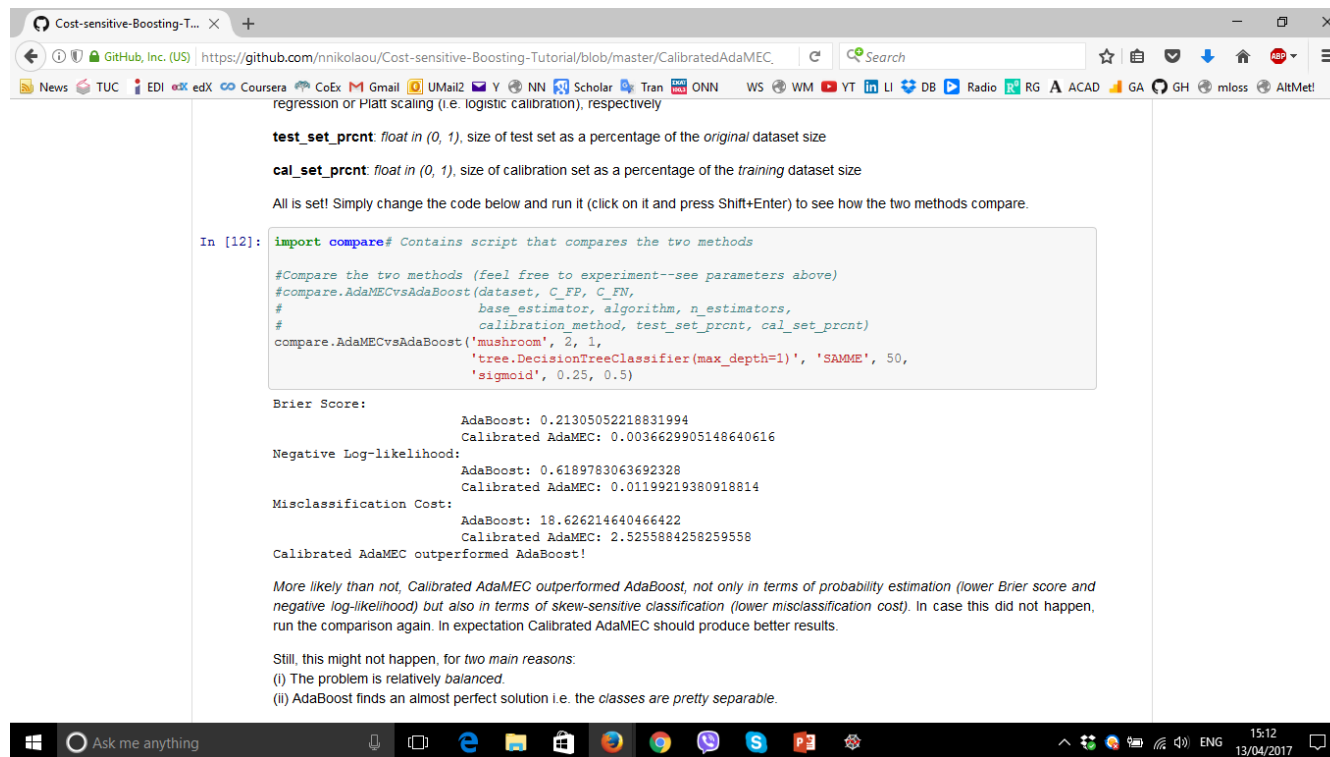
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AdaC2 (Sun et al. 2005, 2007)	✓		✓	
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AdaDB (Landesa-Vázquez & Alba-Castro 2013)	✓	✓		
AdaMEC (Ting 2000, Nikolaou & Brown 2015)	✓	✓	✓	
CGAda (Landesa-Vázquez & Alba-Castro 2012, 2015)	✓	✓	✓	
AsymAda (Viola & Jones 2002)	✓	✓	✓	

So could we just calibrate these last three? **We use “Platt scaling”.**

Q: Sensitive to calibration choices?

A: Check it out on your own!

<https://github.com/nnikolaou/Cost-sensitive-Boosting-Tutorial>



```
regression or Platt scaling (i.e. logistic calibration), respectively

test_set_prnt: float in (0, 1), size of test set as a percentage of the original dataset size
cal_set_prnt: float in (0, 1), size of calibration set as a percentage of the training dataset size

All is set! Simply change the code below and run it (click on it and press Shift+Enter) to see how the two methods compare.

In [12]: import compare# Contains script that compares the two methods

#Compare the two methods (feel free to experiment--see parameters above)
#compare.AdaMECvsAdaBoost(dataset, C_FP, C_FN,
#                          base_estimator, algorithm, n_estimators,
#                          calibration_method, test_set_prnt, cal_set_prnt)
compare.AdaMECvsAdaBoost('mushroom', 2, 1,
                          'tree.DecisionTreeClassifier(max_depth=1)', 'SAMME', 50,
                          'sigmoid', 0.25, 0.5)

Brier Score:
AdaBoost: 0.21305052218831994
Calibrated AdaMEC: 0.0036629905148640616

Negative Log-likelihood:
AdaBoost: 0.6189783063692328
Calibrated AdaMEC: 0.01199219380918814

Misclassification Cost:
AdaBoost: 18.626214640466422
Calibrated AdaMEC: 2.5255884258259558

Calibrated AdaMEC outperformed AdaBoost!

More likely than not, Calibrated AdaMEC outperformed AdaBoost, not only in terms of probability estimation (lower Brier score and negative log-likelihood) but also in terms of skew-sensitive classification (lower misclassification cost). In case this did not happen, run the comparison again. In expectation Calibrated AdaMEC should produce better results.

Still, this might not happen, for two main reasons:
(i) The problem is relatively balanced.
(ii) AdaBoost finds an almost perfect solution i.e. the classes are pretty separable.
```


Results

Isotonic regression > Platt scaling, for larger datasets

Can do better than 50%-50% train-calibration split (problem dependent; see Part II)

(Calibrated) Real AdaBoost > (Calibrated) Discrete AdaBoost...

In summary...

“Calibrated-AdaMEC” was one of the top methods.

1. Take original Adaboost.

2. Calibrate it (we use Platt scaling)

3. Shift the decision threshold.... : $\frac{C_{FP}}{C_{FP} + C_{FN}}$

Consistent with all theory perspectives.

No extra **hyperparameters** added.

No need to retrain if cost ratio changes.

Consistently **top (or joint top)** in empirical comparisons.

Conclusions

We analyzed the cost-sensitive boosting literature

... **15+** variants over **20** years, from **4** different theoretical perspectives

“Cost sensitive” modifications to the original Adaboost are not needed...

... if the scores are properly calibrated,

and the decision threshold is shifted according to the cost matrix.

Relevant publications

- N. Nikolaou and G. Brown, *Calibrating AdaBoost for Asymmetric Learning*, Multiple Classifier Systems, 2015
- N. Nikolaou, N. Edakunni, M. Kull, P. Flach and G. Brown, *Cost-sensitive Boosting algorithms: Do we really need them?*, Machine Learning Journal, Vol. 104, Issue 2, Sept 2016
 - Best Poster Award, INIT/AERFAI summer school in ML 2014
 - Plenary Talk ECML 2016 -- 12/129 eligible papers (9.3%)
 - Best Paper Award 2016, School of Computer Science, University of Manchester
- N. Nikolaou, *Cost-sensitive Boosting: A Unified Approach*, PhD Thesis, University of Manchester, 2016
 - Best Thesis Award 2017, School of Computer Science, University of Manchester



Resources & code

- Easy-to-use but not so flexible ‘Calibrated AdaMEC’ python implementation (scikit-learn style):

<https://mloss.org/revision/view/2069/>

- i-python tutorial for all this with interactive code for ‘Calibrated AdaMEC’, where every choice can be tweaked:

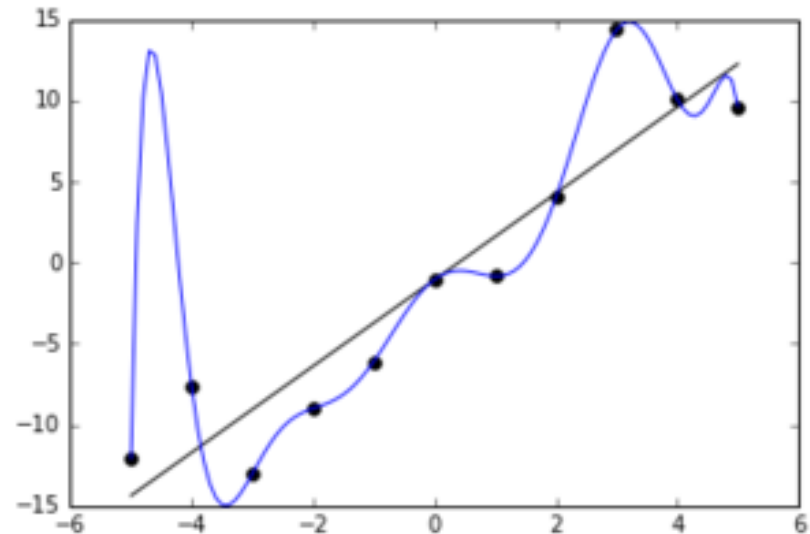
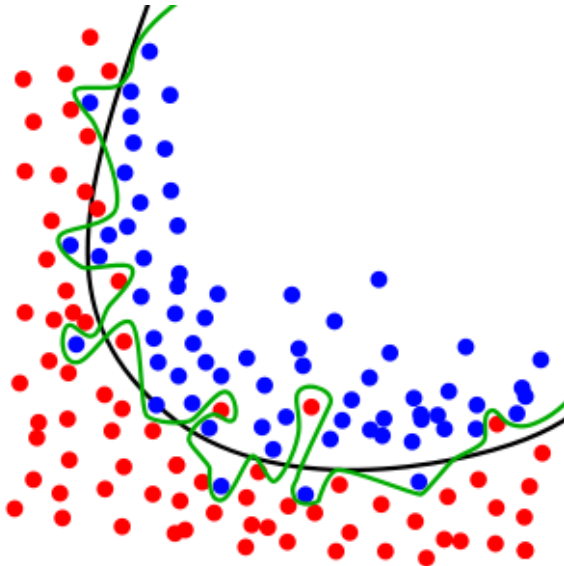
<https://github.com/nnikolaou/Cost-sensitive-Boosting-Tutorial>

Connections to Deep Learning (1)

Both **Boosting** and **Deep Neural Networks** (DNNs) exhibit **very good generalization**...

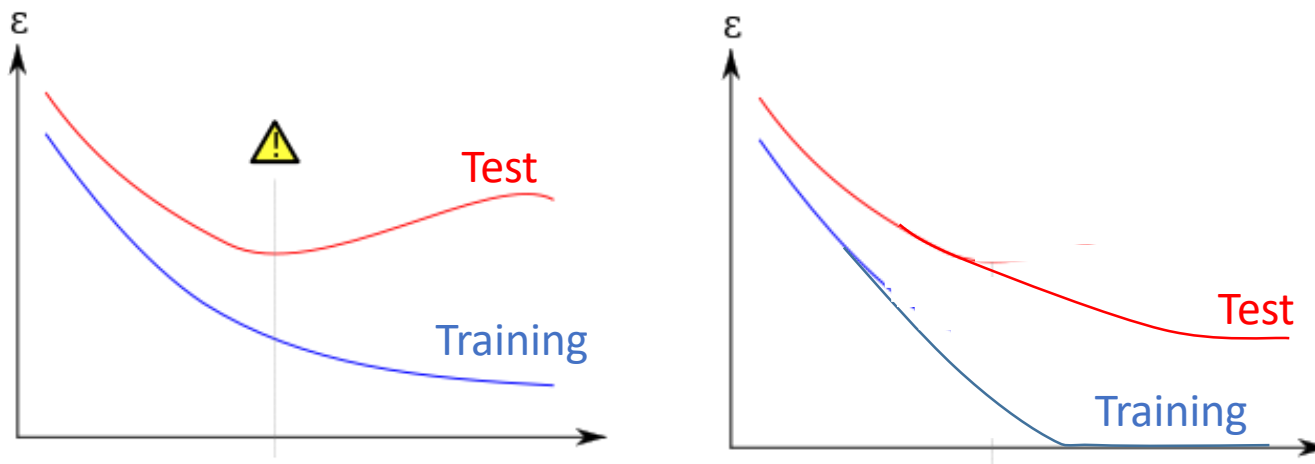
..despite constructing **overparameterized** (drawn from a very rich family) **models**

Too high richness (capacity, complexity, degrees of freedom) of model → **overfitting**



Connections to Deep Learning (2)

Overfitting: fitting the training dataset 'too well', 'memorizing it' rather than 'learning from it', capturing noise as part of the concept to be learned thus failing to generalize to new data (poor performance on test set)



But both **Boosting & DNNs** can **improve fitting the test data even beyond the point of perfectly fitting the training data!**

“Boosting the margin: a new explanation for the effectiveness of voting methods”, Schapire et al. 1997

“Understanding Deep Learning Requires Rethinking Generalization”, Zhang et al, 2017

“Opening the Black Box of Deep Neural Networks via Information”, Shwartz-Ziv & Tishby, 2017

Connections to Deep Learning (3)

The **good classification generalization of DNNs** has been justified through

- **margin maximization:**

“Robust Large Margin Deep Neural Networks”, Sokolic et al., 2017

[Note: As with Boosting]

- **properties of (Stochastic) GD:**

“A Bayesian Perspective on Generalization and Stochastic Gradient Descent”, Smith & Le, 2017

“The Implicit Bias of Gradient Descent on Separable Data”, Soudry et al., 2017

[Note: Boosting also a Gradient Descent process; stochasticity also applied/substituted by other mechanisms]

- **information theory:**

“Opening the Black Box of Deep Neural Networks via Information”, Shwartz-Ziv & Tishby, 2017

[Note: **We are currently applying similar ideas to justify generalization in Boosting-seems to work!**]

Residual Networks (ResNets), a state of the art DNN architecture has been directly **explained through boosting theory**

“Learning Deep ResNet Blocks Sequentially using Boosting Theory”, Huang et al., 2017

Connections to Deep Learning (4)

ResNets also **very good classifiers** but **very poor probability estimators**

“On Calibration of Modern Neural Networks”, Guo et al., 2017

CONJECTURE : Not a coincidence! [direct analogy to boosting]

Similar behaviour in **other architectures**...

“Understanding Deep Learning Requires Rethinking Generalization”, Zhang et al, 2017

“Regularizing Neural Networks by Penalizing Confident Output Distributions”, Pereyra et al., 2017

CONJECTURE: Also not a coincidence! [implicit regularization afforded by GD optimization \equiv margin maximization: good for generalization but scores are distorted towards the extremes]

At any rate, when solving **probability estimation/cost-sensitive** problems using **DNNs** you **should calibrate their outputs!**

End of Part I

Questions?

Part II: Calibrating Online Boosting



Next Step: Online learning

Examples presented **one (or a few) @ a time**

Learner makes **predictions as examples are received**

Each 'minibatch' used to **update model**, then discarded;
constant time & space complexity

Why?

- Data arrive this way (**streaming**)
- Problem (e.g. data distribution) **changes over time**
- To **speed up learning** in big data applications

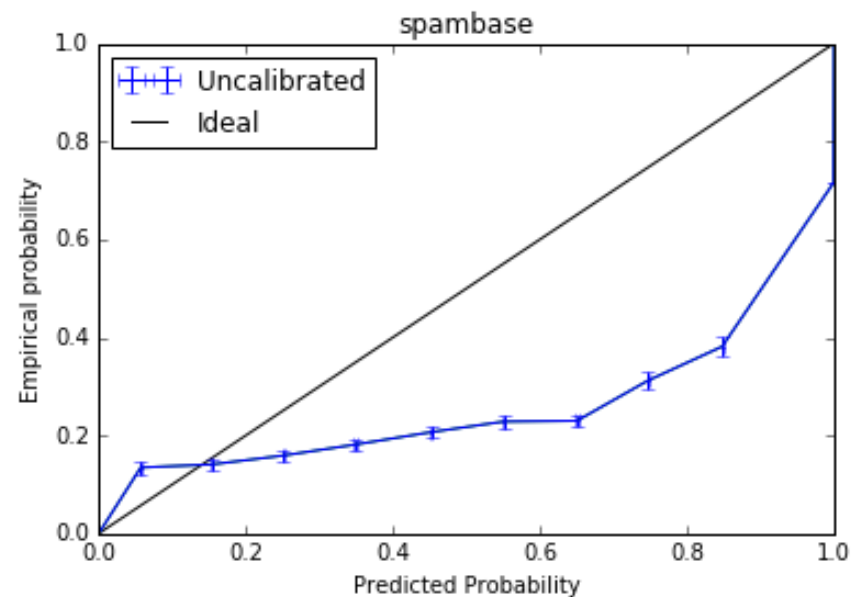
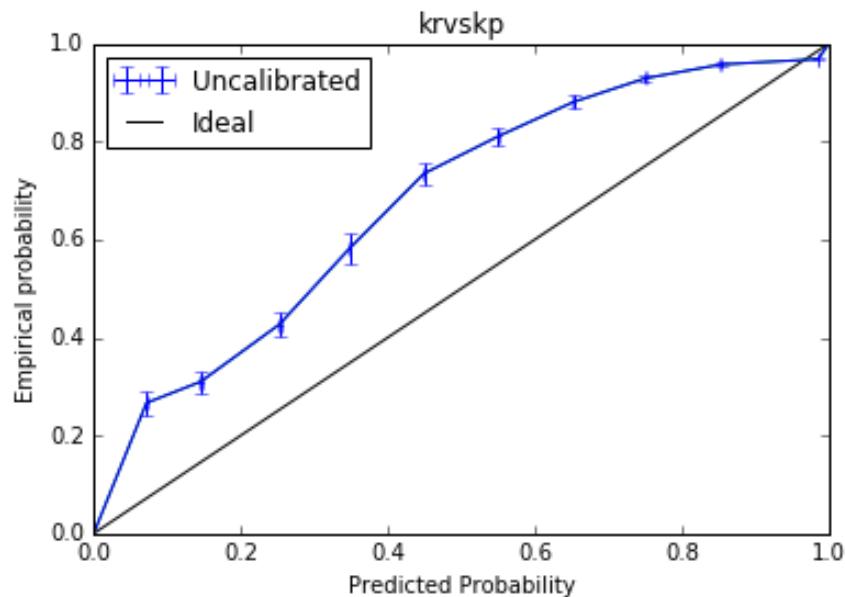
Online learning

For each *minibatch* n do:

1. **Receive** n
2. **Predict label / class probability** of examples in n
3. **Get true label** of examples in n
4. **Evaluate** learner's performance on n
5. **Update learner parameters** accordingly

Online Boosting (Oza, 2004)

Probability estimates -as in AdaBoost- are **uncalibrated**:



How to calibrate online Boosting?

Batch Learning: **reserve part of the dataset** to train calibrator function (logistic sigmoid, if Platt scaling)

Online learning: **cannot do this**; on each minibatch we must **decide** whether to **train ensemble or calibrator**

How to make this decision?

Naïve approach

Fixed Policy: calibrate **every N rounds**

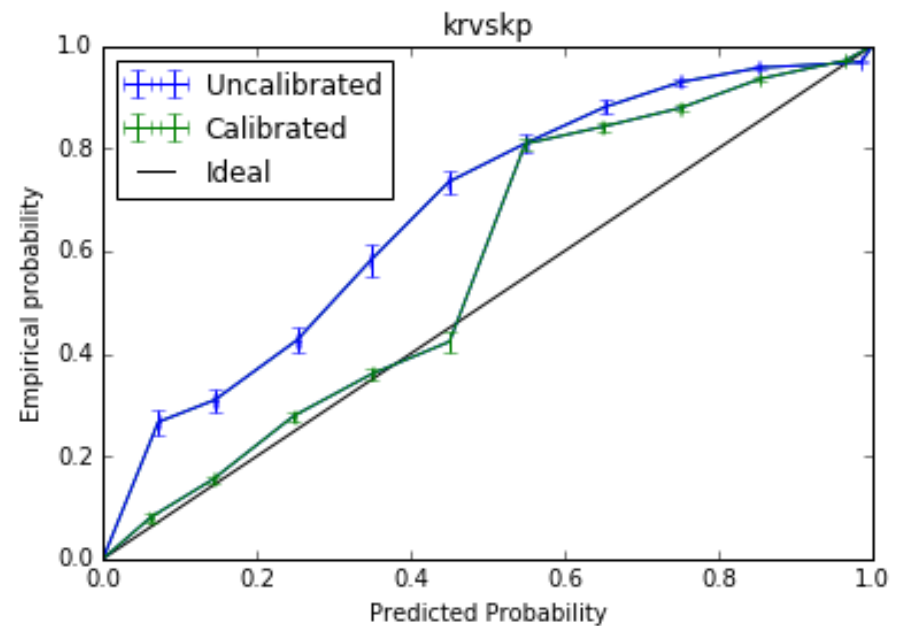
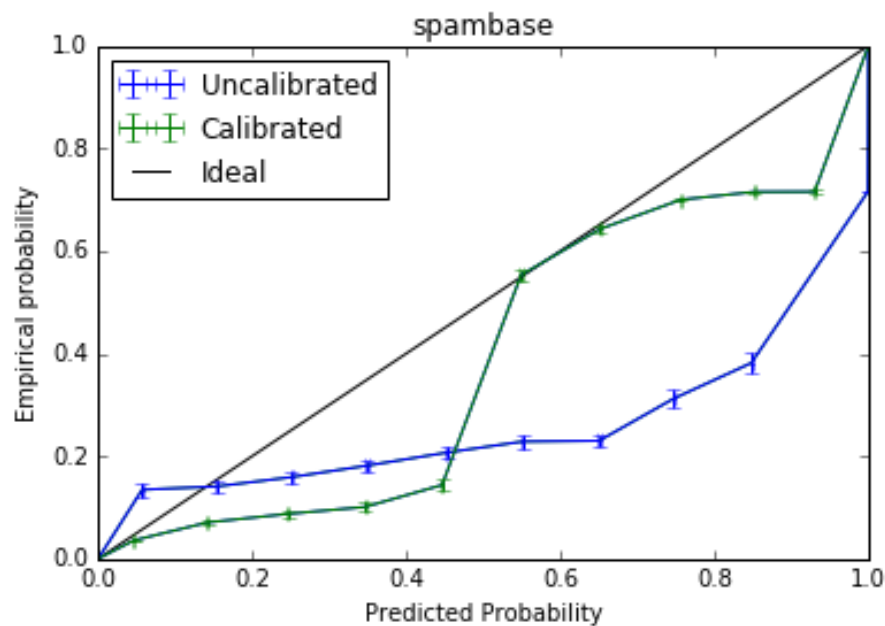
How to pick N ?

- Will depend on **problem**
- Will depend on **ensemble hyperparameters**
- Will depend on **calibrator hyperparameters**
- **Might change** during training...

In batch learning can **choose via cross-validation; not here**

Still, naïve better than nothing

Results with $N = 2$ (**not** necessarily best value):



A more refined approach

- What if we could **learn** a good sequence of alternating between actions?



**Bandit
Algorithms**

Bandit optimization

A **set of actions (arms)** -on each round we choose one

Each action associated with a **reward distribution**

Each time an action taken we **sample** its reward distribution

Sequence of actions that **minimize cumulative regret?**

Exploration vs. Exploitation

In online calibrated boosting:

Two actions: { **train** , **calibrate** }

Reward: **Increase in overall model likelihood** after action

Thompson sampling

A **Bayesian** take on bandits for updating reward distribution

Assume **rewards are Gaussian**; start with **Gaussian prior**,
then **update** using **self-conjugacy of Gaussian distribution**

Take action with **highest posterior reward**

UCB policies

‘Optimism in the face of uncertainty’

Choose not the action with best expected reward, but that with **highest upper bound on reward**

Bounds derived for arbitrary (UCB1, UCB1-Improved) or specific (KL-UCB) reward distributions

Discounted rewards

'Forgetting the past'

Weigh past rewards less; protects from **non-stationarity**

Why non-stationary?

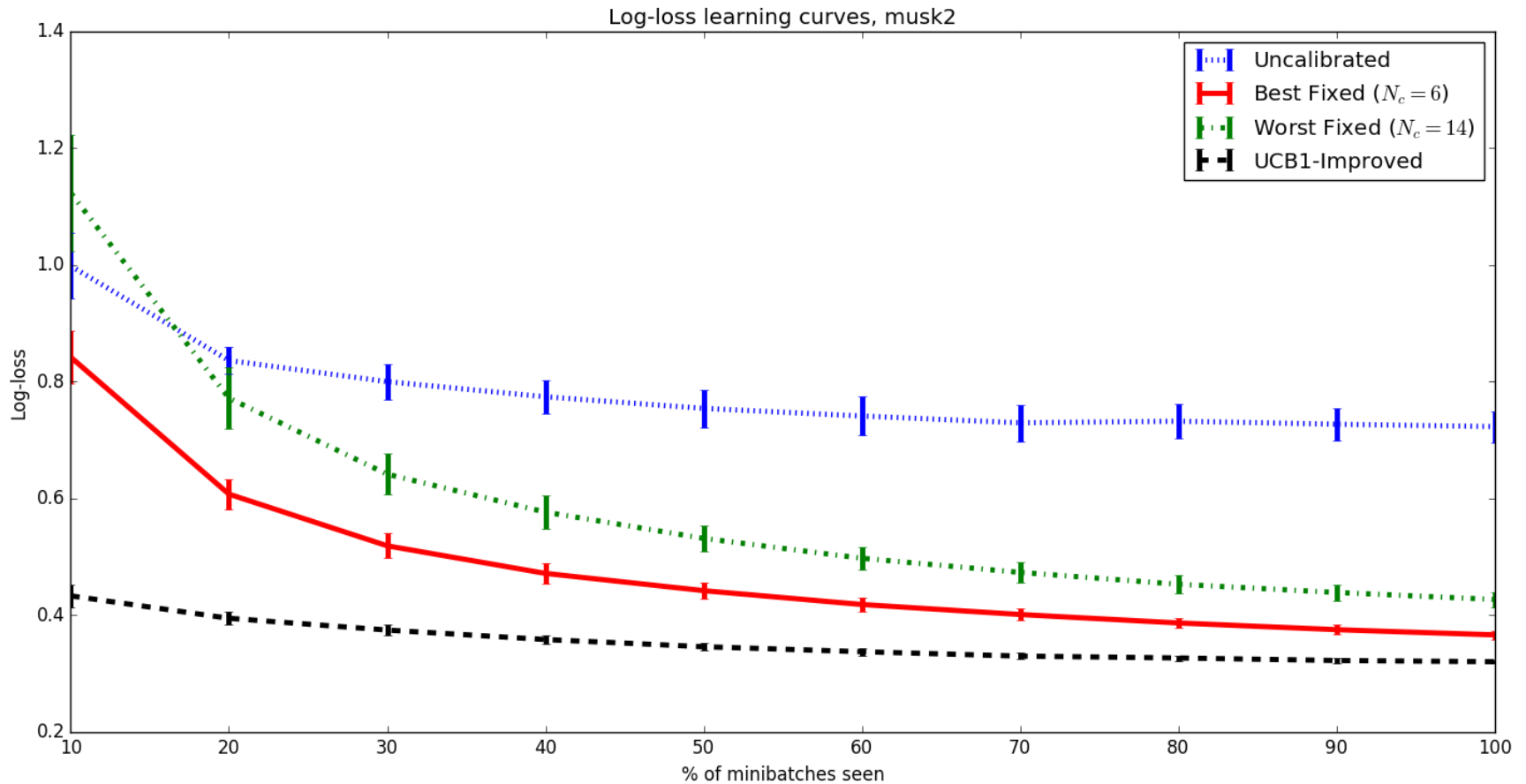
- **Data distribution** might **change**...
- ...most importantly: **reward distributions** will **change**:
if we perform one action many times, the relative reward for performing the other is expected to have increased

Some initial results

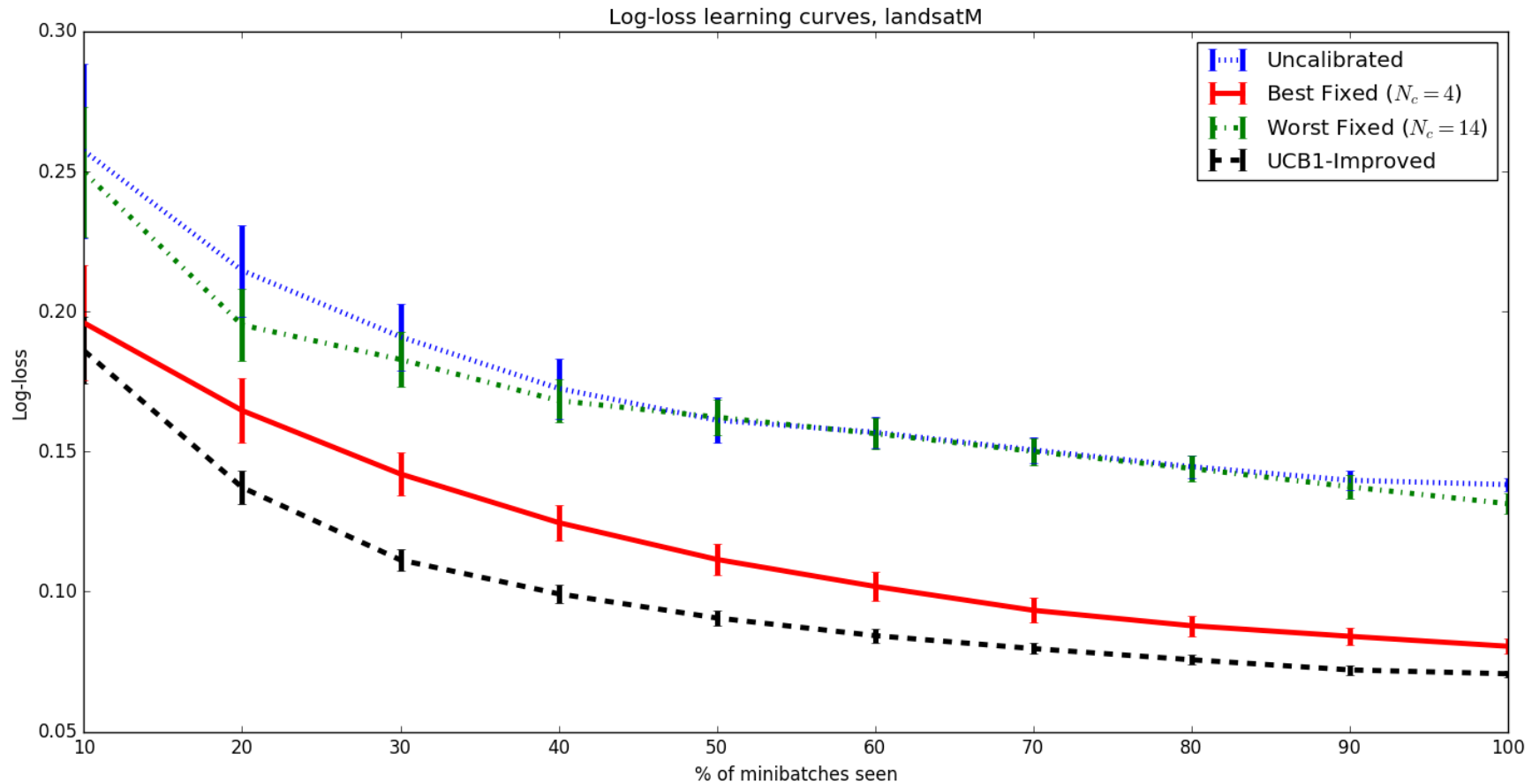
- Uncalibrated
 - vs. 'Every N policies' $N \in \{2, 4, 6, 8, 10, 12, 14\}$
 - vs. UCB1, UCB1-Improved, Gaussian Thompson Sampling
 - vs. Discounted versions of above
- Initial results:
 - **calibrating (even naive)** > not calibrating
 - **non-discounted UCB1 variants** \geq **best** 'Every N ' policy
 - **discounted Thompson Sampling** \geq **best** 'Every N ' policy
 - ... plus no need to set N



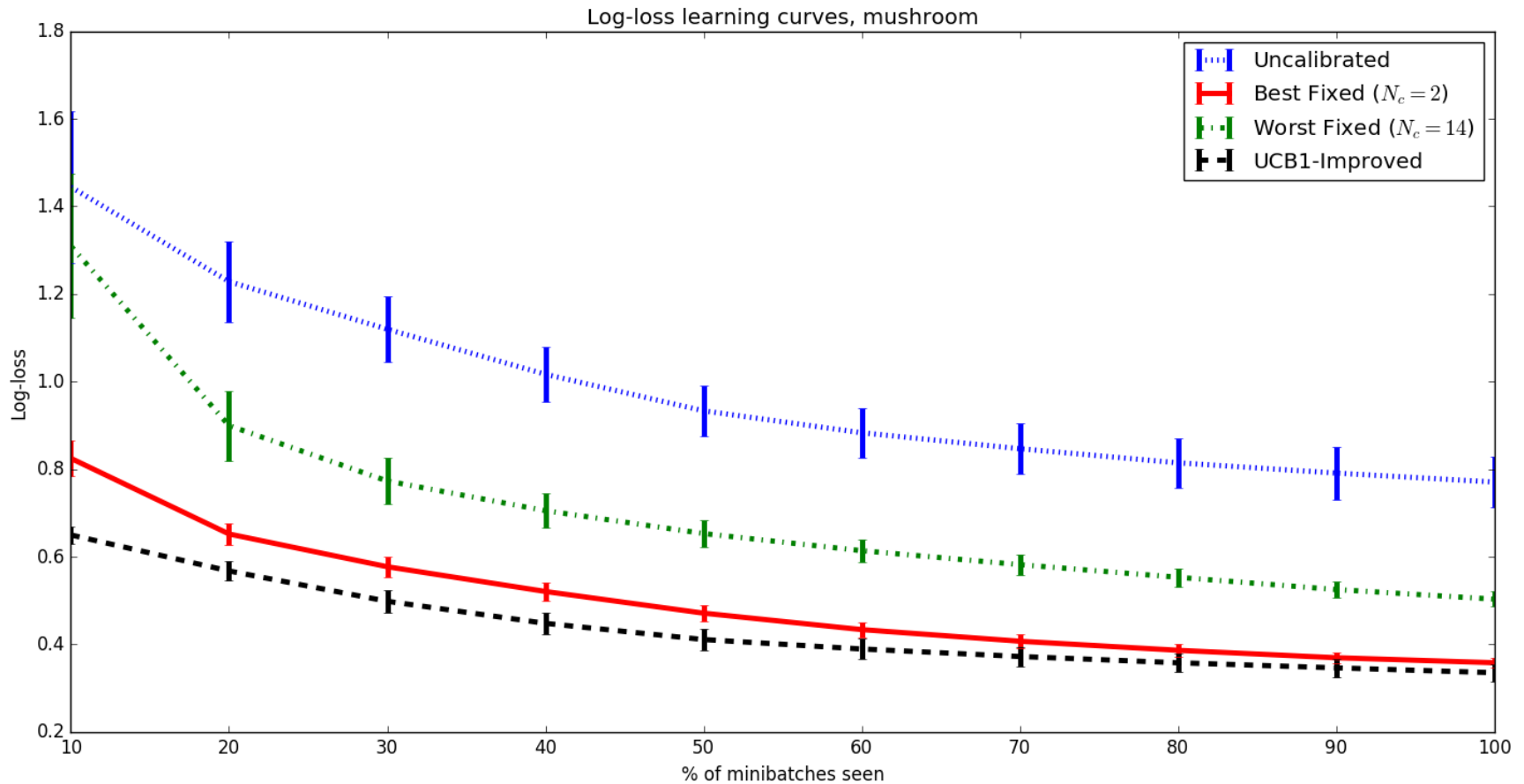
Log-loss learning curves (Impr. UCB1)



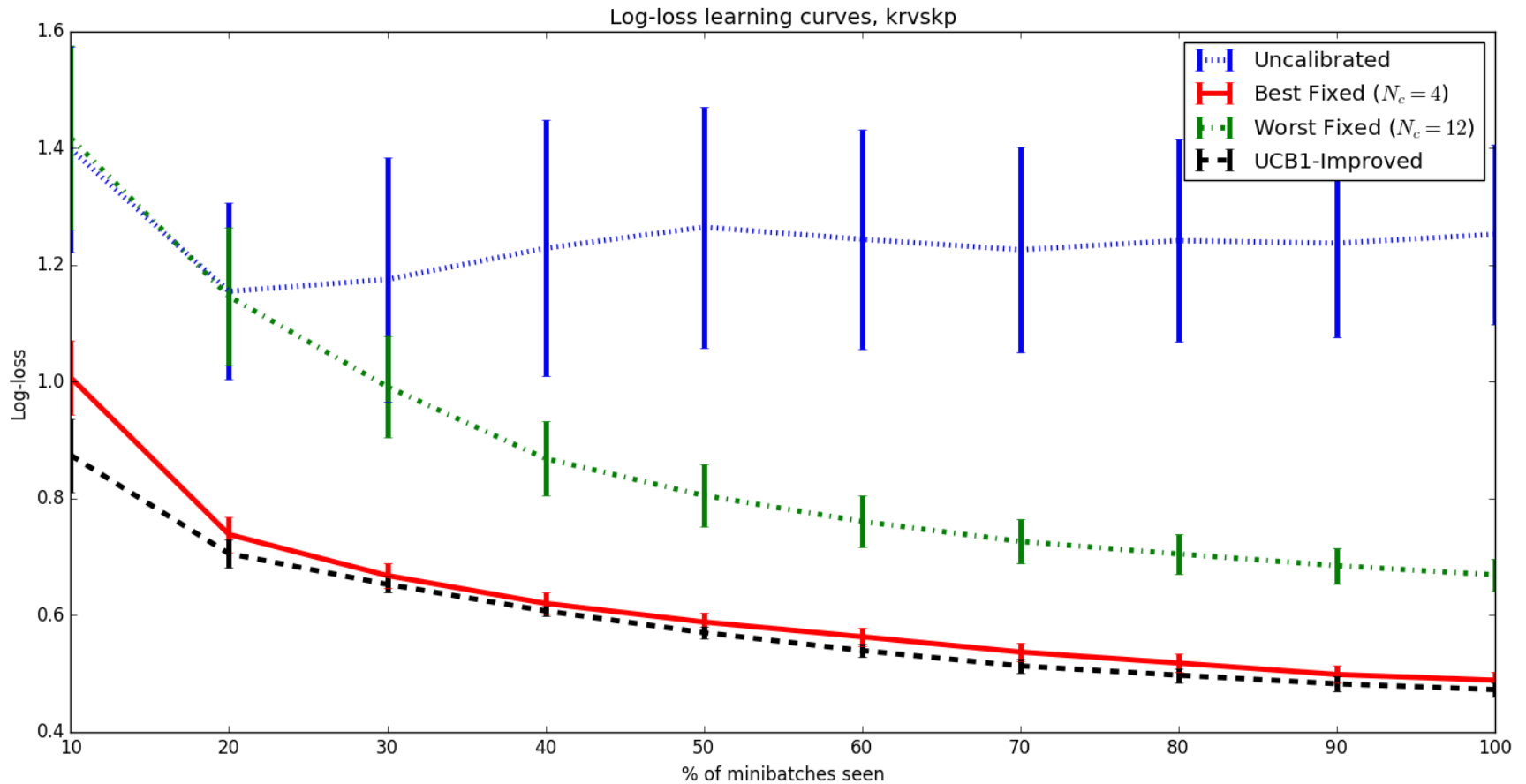
Log-loss learning curves (Impr. UCB1)



Log-loss learning curves (Impr. UCB1)



Log-loss learning curves (Impr. UCB1)



Some Notes

Results shown for ensembles of $M=10$ Naïve Bayes weak learners

Similar results for

other bandit policies

other weak learners

regularized weak learners

varying ensemble sizes

presence of inherent non-stationarity

Also **beats other Naïve policies** (mention)

In summary...

Online Boosting **poor probability estimates**; some **calibration** can improve

Learn a good sequence of calibration / training actions using **bandits**

Online, fast, at least as good as 'best naïve' + adaptive to non-stationarity

Easy to **adapt to other problems** (e.g. cost-sensitive learning)

Robust to ensemble/calibrator **hyperparameters**

Extensions: e.g. **adversarial, contextual, more actions, refine calibration, ...**

Thank you! Ευχαριστώ!

Questions?