A Priori Reasoning for Component-based Software Development*

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Abstract. We believe that the paradigm shift to component-based software development should be accompanied by a corresponding paradigm shift in the underlying approach to specification and reasoning. In this position paper, we propose *a priori reasoning* as a suitable candidate, and outline our approach to specifying and reasoning about components, based on *a priori reasoning*.

1 Introduction

This paper is about what we call *a priori reasoning*. More than that, it is also about why and how *a priori reasoning* can help Component-based Software Development (CBD) achieve its ultimate objective of *third-party assembly*. We will discuss how to specify components, in order that we can reason about them in an *a priori* manner. In particular, we will present a notion of *a priori correctness*, which underpins our approach.

2 Component Specification

Ideally components should be *black boxes*, in order that users can (re)use them without knowing the details of their innards. In other words, the *interface* of a component should provide *all* the information that users need. Moreover, this information should be the *only* information that they need. Consequently, the interface of a component should be the *only* point of access to the component. It should therefore contain all the information that users need to know about the component's *operations*, i.e. what its code does, and its *context dependencies*, i.e. how and where the component can be deployed. The code, on the other hand, should be completely inaccessible (and invisible), if a component is to be used as a black box.

The *specification* of a component is therefore the specification of its *interface*, which must consist of a precise definition of the component's operations and context dependencies, and nothing else.

* This paper is a variation of the paper K.-K. Lau and M. Ornaghi, A Formal Approach to Software Component Specification, in D. Giannakopoulou, G.T. Leavens and M. Sitaraman, editors, Proceedings of Specification and Verification of Component-based Systems Workshop at OOPSLA2001, pages 88–96, Tampa, USA, October 2001. It was also presented at the Third International Workshop on (Constraint) Logic Programming and Software Engineering, 28 July 2002, Copenhagen, Denmark.

3 A Posteriori Reasoning

Before introducing *a priori reasoning*, it is illuminating to first consider its opposite number, *a posteriori reasoning*. This is well illustrated by many *verification-based* methods for program construction, which take the '*posit-and-see*' approach:

> Given the specification for a program, *first* posit a program, *then* see if the program can be verified to be correct (with respect to the given specification).

This is what we call *a posteriori reasoning*: reasoning about correctness (or other properties) takes place *after* the program or component has been constructed. It does not offer any help with the construction *a priori*. In particular, if the construction is a composition or an assembly of components, *a posteriori reasoning* does not offer any *assembly guide*, i.e. how to choose the right components (so that their composition will meet the requisite specification of the composite).

4 A Priori Reasoning

By contrast, *a priori reasoning* takes places *before* the construction takes place, and should therefore provide an *assembly guide* for component composition.

For CBD, *a priori reasoning* would work as follows:

- it requires that it is possible to show *a priori* that the individual components in question are *correct* (with respect to their own specifications);
  (This enables us to do *component certification*, see below.)
- it then offers help with reasoning about the *composition* of these components:
  - to guide their composition in order to meet the specification of a larger system;
  - to predict the precise nature of any composite, so that the composite can in turn be used as a unit for further composition.

  (This enables us to do *system prediction*, see below.)

5 Predictable Component Assembly

We believe that *a priori reasoning* addresses an open problem, viz. *predictable component assembly*. It does so because it enables component certification and system prediction.

Consider Figure 1. Two components A and B each have their own interface and code. If the composition of A and B is C, can we determine or deduce the interface and

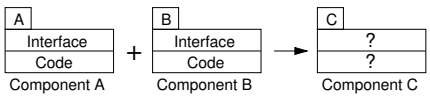

Fig. 1. Predicting component assembly.

code of C from those of A and B? The answer lies in component certification.

Component Certification Certification should say what a component does (in terms of its *context dependencies*) and should guarantee that it will do precisely this (for all contexts where its dependencies are satisfied). A certified component, i.e. its interface, should therefore be specified properly, and its code should be verified against its specification. Therefore, when using a certified component, we need only follow its interface. In contrast, we cannot trust the interface of an uncertified component, since it may not be specified properly and in any case we should not place any confidence in its code.

In the context of *a priori reasoning*, a certified component A is *a priori correct*. This means that:

- A is guaranteed to be correct, i.e. to meet its own specification;
- A will always remain correct even if and when it becomes part of a composite.

This is illustrated by Figure 2, where component A has been certified, so we know how

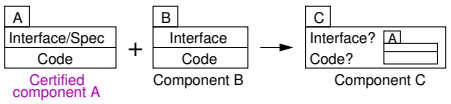

Fig. 2. Component certification.

it will behave in the composite C.

However, we do not know how B will behave in C, since it is not certified. Consequently, we cannot expect to know C's interface and code from those of A and B, i.e. we cannot predict the result of the assembly of A and B.

System Prediction For system prediction, obviously we need *all* constituent components to be certified (*a priori correct*). Moreover, for any pair of certified components A and B whose composition yields C:

- *before* putting A and B together, we need to know what C will be;
- and furthermore, we need to be able to certify C.

This is illustrated by Figure 3. The specification of C must be predictable prior to com-

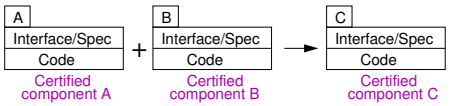

Fig. 3. System prediction.

position. Moreover, we need to know how to certify C properly, and thus how to use C in subsequent composition. *A priori correctness* is just what we need in order to do system prediction.

6 A Priori Reasoning in Modular Specification and Verification

A degree of a priori reasoning is carried out in current approaches to modular (formal) specification and verification, e.g. [9, 14], which use *modular reasoning*. This is specification-based reasoning that tries to say before running the software whether it will behave as specified or not (subject to relevant assumptions). This is illustrated in Figure 4. Before a composite module C is deployed, we can predict whether it will

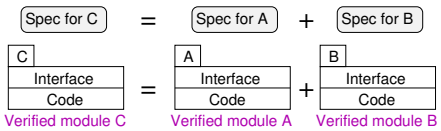

Fig. 4. Module composition.

work according to its specification. For example, if component modules, say A and B, are to be used in C, the correctness of C is established based on the specifications of A and B (even before A and B have been implemented). The components A and B are then verified independently. The contexts of A and B are taken in account when using and verifying A and B.

Thus modular reasoning is *a priori* in nature. It predicts correctness, based on specification. This kind of prediction is we believe subtly different from the prediction that we intend to convey in Figure 3, which predicts specification, based on (certified) correctness (we will discuss this in Section 12).

7 Specifying Components for A Priori Reasoning

In the rest of this paper, we outline how we specify components, so that we can carry out a priori reasoning about their construction and composition. Diagrammatically, our component looks like Figure 5, and in the subsequent sections, we will explain the key

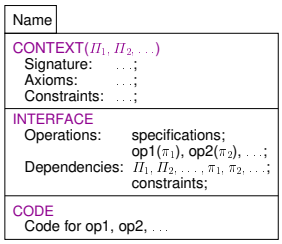

Fig. 5. Ingredients of a component.

ingredients, viz. the *context* and the *interface*, and their specifications.

We should point out that this is work in progress, so we do not yet have all the answers, so to speak.

8 Context

A component is defined in a *problem domain*, or a *context*. We will represent a context as a full first-order logical theory with an intended (mathematical) model.

Signature and Axioms A *context* $\mathcal{C} = \langle \Sigma, X \rangle$ is composed of a *signature* Σ (containing *sort* symbols, *function* declarations and *relation* declarations) and a finite or recursive set X of Σ-axioms. A context axiomatises a problem domain and thus enables us to reason about it. More specifically, a context contains the *abstract data types* (ADTs) and all the concepts that are needed to build a model of the application at hand. A context is thus a (first-order) theory with an intended model.

We distinguish between *closed* and *open* (or *parametric*) contexts. A context $\mathcal{C} = \langle \Sigma, X \rangle$ is *closed* if its signature Σ does not contain any parameters. In this case, $\mathcal{C}$'s axioms X have one fixed model. By contrast, a context $\mathcal{C} = \langle \Sigma, X \rangle$ is *open* if its signature Σ contains parameters. In this case, $\mathcal{C}$'s axioms X have many potential models, depending on the parameters in the signature Σ.

Example 1. A simple example of a closed context is first-order arithmetic $\mathcal{NAT} = \langle \Sigma_{PA}, PA \rangle$. Σ_{PA} contains the unary function s (successor) and the binary functions $+$ (sum) and $*$ (product). PA contains the usual Peano's axioms for $s, +, *$ (and all the instances of the first-order induction schema).

CONTEXT $\mathcal{NAT}$;

SIGNATURE:

Sorts: N;

Functions: $0 : [\,] \to N$;
$s : [N] \to N$;
$+, * : [N, N] \to N$;

AXIOMS: $\{s\}$: $\forall x : N \,.\, \neg s(x) = 0$;
$\forall x, y : N \,.\, s(x) = s(y) \to x = y$;
$\{+\}$: $\forall x : N \,.\, x + 0 = x$;
$\forall x, y : N \,.\, x + s(y) = s(x + y)$;
$\{*\}$: $\forall x : N \,.\, x * 0 = 0$;
$\forall x, y : N \,.\, x * s(y) = (x * y) + x$.

The standard structure of natural numbers is the intended model of $\mathcal{NAT}$.

Example 2. A simple example of an open context is the following, which axiomatises lists with generic elements X and a generic total ordering $\lhd$ on X.

CONTEXT $\mathcal{LIST}(X, \lhd : [X, X])$;

IMPORT: $\mathcal{NAT}$;

SIGNATURE:

Sorts : X, L;

Functions: $nil : [\,] \to L$;
$| : [X, L] \to L$;
$nocc : [X, L] \to N$;

Relations: $pos : [X, N, L]$;

AXIOMS:
$\{nil, |\}$: $\forall x, y, z : X,\ \forall j, k, l : L\ .$
$(\neg nil = x|j \wedge (y|k = z|l \rightarrow y = z \wedge k = l))$;
$\{nocc\}$: $\forall x : X\ .\ nocc(x, nil) = 0$;
$\forall x, y : X,\ \forall l : L\ .$
$x = y \rightarrow nocc(x, y.l) = nocc(x, l) + 1$;
$\forall x, y : X,\ \forall l : L\ .$
$\neg x = y \rightarrow nocc(x, y.l) = nocc(x, l)$;
$\{pos\}$: $\forall x : X,\ \forall l : L\ .$
$(pos(x, 0, l) \leftrightarrow \exists y : X,\ j : L\ .\ l = y|j \wedge x = y)$;
$\forall x : X,\ \forall l : L\ .$
$(pos(x, s(i), l) \leftrightarrow \exists y : X,\ j : L\ .$
$l = y|j \wedge pos(x, i, j))$.

The context (ADT) $\mathcal{NAT}$ is imported, together with its signature Σ_{PA} and axioms PA.

nil and $|$ are the *constructors* for the sort L of lists of elements of sort X. (For an element x and a list y, $x|y$ stands for the list with head x and tail y.) Their axioms are the list *constructor axioms* (plus structural induction).

$pos(x, i, l)$ means that the element x occurs at position i in the list l, where positions start from 0.

$nocc(x, l)$ is the number of occurrences of the element x in the list l.

Constraints In an open context, some of the parameters in the signature may not be instantiated just anyhow. In fact their instantiation must be subject to strictly defined constraints.

Example 3. In the context $\mathcal{LIST}(X, \lhd : [X, X])$, in order to ensure that $\lhd$ is a total ordering, we have to add the following *constraints*:

CONTEXT $\mathcal{LIST}(X, \lhd : [X, X])$;
IMPORT: $\mathcal{NAT}$;
SIGNATURE:
Sorts : X, L;
Functions: ...
Relations: ...
AXIOMS: ...
CONSTRAINTS: $\forall x, y, z : X\ .\ (x \lhd y \wedge y \lhd x) \leftrightarrow x = y$;
$\forall x, y, z : X\ .\ (x \lhd y \wedge y \lhd z) \rightarrow x \lhd z$;
$\forall x, y, z : X\ .\ x \lhd y \vee y \lhd x$.

The purpose of constraints is to filter out illegal parameters of the context: only parameters that satisfy the constraints are allowed. For example, if in the context $\mathcal{LIST}($ X, $\lhd$: $[X, X])$, we want to substitute X by the sort N of natural numbers, and the ordering $\lhd$ by $\leq$ on N, then we can express this as a *closure* (or *instance*):

CLOSURE $\mathcal{NATLIST}$ OF $\mathcal{LIST}(X, \lhd : [X, X])$;
CLOSE: X BY N;
$\lhd$ BY $\forall x, y : N\ .\ (x \lhd y \leftrightarrow x \leq y)$.

This closure of the context $\mathcal{LIST}(X, \lhd : [X, X])$ satisfy the constraints of the context since $\leq$ is a total ordering on N.

In this example, we have closed X and $\lhd$ within $\mathcal{LIST}$ itself, for simplicity. In general, of course, they could also be closed within another context $\mathcal{C}$, after importing $\mathcal{LIST}$ into $\mathcal{C}$.

Obviously constraints define context dependencies.

9 Interface

The interface of a component is defined in the context of the component. The interface is the only part of the component that is visible to the users, and it should provide all the information that the users need in order to deploy the component. Since the interface is defined within the context, the latter should be regarded as part of the former. As we already made clear, the interface should contain specifications for the operations, and the context dependencies, of the component.

Operations In the interface, operations are represented by their specifications. In a context $\langle \Sigma, X \rangle$, a specification of a new (relation) symbol r is a set of axioms that define r in terms of the symbols of the signature Σ. For example, suppose in $\mathcal{LIST}$ we have operations for sorting, such as *insertion sort* and *bubble sort*. The specification for these two operations are as follows:[1]

$$\forall l : L \,.\, ord(l) \leftrightarrow$$
$$\forall i : N,\ \forall x, y : X \,.\, ((pos(x, i, l) \wedge pos(y, s(i), l)) \rightarrow x \lhd y)$$
$$\forall j, k : L \,.\, perm(j, k) \leftrightarrow \forall x : X \,.\, nocc(x, j) = nocc(x, k)$$
$$\forall j, k : L \,.\, sort(j, k) \leftrightarrow perm(j, k) \wedge ord(k)$$
$$\forall j, k, l : L \,.\, ord(j) \wedge ord(k) \rightarrow$$
$$(merge(j, k, l) \leftrightarrow ord(l) \wedge perm(j \| k, l)).$$

We represent operations as logic programs. For example, the operations *insertion sort* and *bubble sort* are represented by the following logic programs:

Operation: insertionSort($merge$)
$sort([\,], [\,]) \leftarrow$
$sort(x.j, l) \leftarrow sort(j, k), merge([x], k, l)$

Operation: bubbleSort($\lhd$)
$sort([\,], [\,]) \leftarrow$
$sort(x.j, y.l) \leftarrow part(x.j, [y], k), sort(k, l)$
$part([\,], [\,], [\,]) \leftarrow$
$part([x], [x], [\,]) \leftarrow$
$part(x.j, [x], y.l) \leftarrow x \lhd y, part(j, [y], l)$
$part(x.j, [y], x.l) \leftarrow y \lhd x, part(j, [y], l)$

The operation insertionSort computes the relation $sort$ (as specified by the specification given above) in terms of the relation $merge$ (also as specified above). It therefore

[1] For lists j and k, $j \| k$ stands for their concatenation.

needs a program for $merge$ in order to complete the sorting operation. As a result insertionSort has $merge$ as a parameter, hence we write insertionSort($merge$). In any context that is a closure (instance) of $\mathcal{LIST}$, insertionSort will need a program for $merge$.

Thus parameters to operations also define context dependencies.

By contrast, the operation bubbleSort has only the parameter $\lhd$, which is the parameter of the context. So bubbleSort will work for any context in which $\lhd$ is instantiated (closed) by any total ordering.

Context Dependencies These consist of the (global) parameters in the signature of the component, the (local) parameters of the operations, together with the constraints in the context.

So now we can define the context dependencies completely in a component.

10 Code

The code should be inaccessible (invisible) to the user. It is usually binary. However, if we allow parameters in the operations, then the code has to be source code, which has to be instantiated before execution.

If the source code is available, then the user or the developer can also verify its correctness with respect to the specifications in the context.

11 A Priori Correctness

In our work the basis for a priori reasoning is *a priori correctness*. So having laid out the specification of a component, we now turn to the definition of a priori correctness of a component. Specifically, we consider a notion of a priori correctness of the operations in a component, that we call *steadfastness*.

Steadfastness A *steadfast* operation (program) Op is one that is correct (with respect to to its specification) in each intended model of the context $\mathcal{C}$ of the component. Since the (reducts of the) intended models of its specialisations and instances are intended models of $\mathcal{C}$, a steadfast program Op is correct, and hence correctly reusable, in all specialisations and instances of $\mathcal{C}$.

A formalisation of steadfastness is given in [8], with both a model-theoretic, hence *declarative*, characterisation and a proof-theoretic treatment of steadfastness. Here we give a simple example (taken from [8]) to illustrate the intuition behind steadfastness.

Example 4. Consider the following component:
where the open context $\mathcal{ITER}(D, \circ, e)$ is defined as follows:

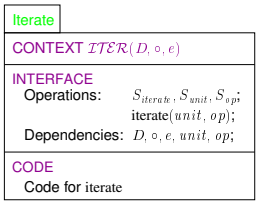

Fig. 6. The Iterate component.

CONTEXT $\mathcal{ITER}(D, \circ, e)$;
IMPORT: $\mathcal{NAT}$;
SIGNATURE:
Sorts: D;
Functions: $e : [\,] \to D$;
$\circ : [D, D] \to D$;
$\times : [D, N] \to D$;
AXIOMS: $\forall x : D\,.\ \times(x, 0) = e$;
$\forall x : D,\ \forall n : N\,.\ \times(x, s(n)) = \times(x, n) \circ x.$

where $\mathcal{NAT}$ is the closed context for first-order Peano arithmetic defined in Example 1.

In the open context $\mathcal{ITER}(D, \circ, e)$:

(i) D is a (generic) domain, with a binary operation $\circ$ and a distinguished element e;
(ii) the usual structure of natural numbers is imported;
(iii) the function symbol $\times$ represents the iteration operation $\times(a, n) = e \circ a \underbrace{\circ \cdots \circ}_{(n \text{ times})} a$.

We can use the Iterate component to iterate n times a binary operation $\circ$ on some (generic) domain D.

Suppose we specify the $iterate$ operation by the following relation:

$$S_{iterate}: \qquad iterate(x, n, z) \leftrightarrow z = \times(a, n) \tag{1}$$

Consider the operation iterate($unit$, op) defined by the following logic program:

Operation: iterate($unit$, op)
$iterate(a, 0, v) \leftarrow unit(v)$
$iterate(a, s(n), v) \leftarrow iterate(a, n, w), op(w, a, v)$

where s is the successor function for natural numbers, and the relations $unit$ and op are specified in $\mathcal{ITER}$ by the specifications:

$$\begin{array}{lll} S_{unit}: & unit(u) & \leftrightarrow u = e \\ S_{op}: & op(x, y, z) & \leftrightarrow z = x \circ y \end{array} \tag{2}$$

The operation iterate($unit$, op) is defined in terms of the parameters $unit$ and op. If we can assume that operations for $unit$ and op are a priori correct, i.e. they are correct with respect to their specifications (2) in *any* interpretation of $\mathcal{ITER}$, then we can prove

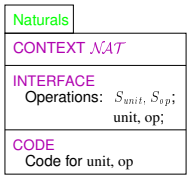

Fig. 7. The Naturals component.

that the operation iterate($unit$, op) is *steadfast*, i.e. it is always correct with respect to (1) (and (2)).

For example, suppose we have a component Naturals as shown in Figure 7, in which the context is $\mathcal{NAT}$, and the operations unit and op are specified as follows:

$$\begin{array}{lll} S_{unit}: & unit(u) & \leftrightarrow u = 0 \\ S_{op} \;\; : & op(x,y,z) & \leftrightarrow z = x + y \end{array} \tag{3}$$

and defined as follows:

Operation:- unit
$unit(0)$.

Operation:- op
$op(x,y,z) \leftarrow z = x + y$

Then in Naturals, unit and op are (trivially) a priori correct with respect to to their specifications (3), and if we compose the components Iterate and Naturals, the operation iterate in the composite Iterate+Naturals will be fully instantiated (and therefore executable), and more importantly it will be correct with respect to its specification (1) (and (2)).

The composition here is of course just the simple closure operation on Iterate, but it is sufficient to illustrate the idea of a priori reasoning. In this closure of Iterate, D is the set of natural numbers, $\circ$ is $+$, e is 0, and $\times(a,n) = 0 + a + \cdots + a = na$. Consequently, the specification $S_{iterate}$ (1) specialises to $iterate(x,n,z) \leftrightarrow z = na$, and similarly S_{unit} (in (2)) specialises to $unit(u) \leftrightarrow u = 0$ (in (3)), and S_{op} (in (2)) to $op(x,y,z) \leftrightarrow z = x + y$ (in (3)). Since, the operations unit and op are correct with respect to their (specialised) specifications (3), the operation (iterate($unit$, op)$\cup$ unit $\cup$ op) will compute na, and is correct with respect to its (specialised) specification in Iterate+Naturals.

To illustrate the correct reusability of the iterate operation in Iterate, suppose now

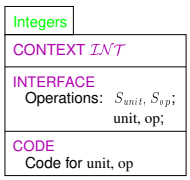

Fig. 8. The Integers component.

we have a component Integers as shown in Figure 8, where the operations unit and op are specified by:

$$\begin{array}{lll} S_{unit}: & unit(u) & \leftrightarrow u = 0 \\ S_{op} \;: & op(x,y,z) & \leftrightarrow z = x - y \end{array} \tag{4}$$

and defined by:

Operation:- unit
$unit(0).$

Operation:- op
$op(x,y,z) \leftarrow z = x - y$

Obviously the operations unit and op in Integers are a priori correct with respect to their specifications (4). We can compose Iterate and Integers by a closure operation on Iterate, and get a correct iterate operation in the composite Iterate+Integers.

In Iterate+Integers, D is the set of integers, $\circ$ is $-$, e is 0, $\times(a,n) = 0 - a - \cdots - a = -na$, and the specification $S_{iterate}$ ((1) in Iterate) specialises to $iterate(x,n,z) \leftrightarrow z = -na$, S_{unit} (in (2)) specialises to $unit(u) \leftrightarrow u = 0$ (in (4)), and S_{op} (in (2)) to $op(x,y,z) \leftrightarrow z = x - y$ (in (4)). Since unit and op are correct with respect to their specifications (4), the operation (iterate$(unit, op)\cup$unit$\cup$op) computes $-na$ for an integer a, and is correct with respect to its (specialised) specification in Iterate+Integers.

The iterate operation is thus a priori correct in Iterate and we say it is *steadfast*. It can be correctly reused in any composite with operations for unit and op as long as these operations are in turn steadfast.

The component Iterate has no constraints in its context dependencies. To further illustrate the notion of steadfastness, we now consider a component whose context dependencies include constraints.

Example 5. Consider the component Iterate* (Figure 9) obtained from Iterate (Figure

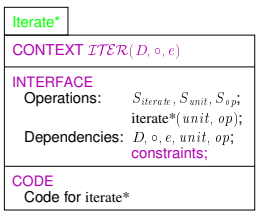

Fig. 9. The Iterate component.

6) by adding the following constraints to its context dependencies:

$$\begin{array}{l} \forall x : D \,.\, e \circ x = x \\ \forall x, y, z : D \,.\, x \circ (y \circ z) = (x \circ y) \circ z \end{array} \tag{5}$$

and by replacing the iterate operation in Iterate by the following operation iterate*:

Operation: iterate*$(unit, op)$
$iterate(a, 0, v) \leftarrow unit(v)$
$iterate(a, n, v) \leftarrow m + m = n, iterate(a, m, w),$
$\quad op(w, w, v)$
$iterate(a, n, v) \leftarrow m + s(m) = n, iterate(a, m, w),$
$\quad op(w, w, z), op(z, a, v)$

The operation iterate* has the same specification $S_{iterate}$ (1) as iterate in Iterate, but it computes the relation $iterate$ more efficiently than iterate: the number of recursive calls is linear in iterate*, whereas it is logarithmic in iterate. However, iterate* would *not* be steadfast in Iterate. For example, if we were to use iterate* in place of iterate in Iterate, then iterate* would be correct with respect to (1) and (2) in Iterate+Naturals, but it would not be correct with respect to (1) and (2) in Iterate+Integers, where, for instance, for $iterate(a, s(\ (s(s(0)))), v)$, iterate* would compute 0 instead of the correct answer $-4a$. Thus despite the a priori correctness of unit and op in both Naturals and Integers, iterate* would not be correct in both Iterate+Naturals and Iterate+Integers. Therefore iterate* would *not* be steadfast in Iterate.

The reason for this is that in Iterate*, the constraints (5) require that the parameters e and $\circ$ of the context satisfy the unit and associativity axioms. These imply that

$$\begin{cases} \times(a, n) = \times(a, n \div 2) \circ \times(a, n \div 2) \circ a & \text{if } n \text{ is odd} \\ \times(a, n) = \times(a, n \div 2) \circ \times(a, n \div 2) & \text{if } n \text{ is even} \end{cases}$$

which means that whenever $\circ$ is associative, $\times$ can be computed in logarithmic time. So, if we were to use iterate* in place of iterate in Iterate, then iterate* would be correct in Iterate+Naturals because here (D is the set of natural numbers) e is 0, $\circ$ is $+$, and so they actually satisfy the constraints (5) anyway, even though these constraints are not present in Iterate. On the other hand, iterate* would not be correct in Iterate+Integers because here (D is the set of integers) e is 0, $\circ$ is $-$, and since $-$ is not associative, they do not satisfy (5).

However, we can prove that iterate* is steadfast in Iterate*, again assuming a priori correctness of operations for unit and op defined in some other component. It will be correct in any composite Iterate*+C as long as C satisfies the constraints (5) in the context dependencies of Iterate*. For example, as can be seen from the above discussion, iterate* will be correct in Iterate*+Naturals since $+$ is associative. For something different, suppose Matrices is a component with a context of m-dimensional square matrices. Then in the composite Iterate*+Matrices, D is the set of m-dimensional square matrices, e is the m-dimensional identity matrix, and since matrix multiplication $\times$ is associative, iterate* will be correct, where op computes matrix products.

12 Discussion

Since a steadfast program is correct, and hence correctly reusable, in all specialisations and instances of its context, a component with steadfast operations, which we will call a *steadfast component*, when composed with another steadfast component will also be

steadfast. In other words, steadfastness is not only *compositional*, but is also preserved through *inheritance* hierarchies.

Consequently, in the context of system prediction (as shown in Figure 3) when composing steadfast components, not only can we be sure that the composite will be steadfast, but we can also predict the specification of the composite. This is illustrated

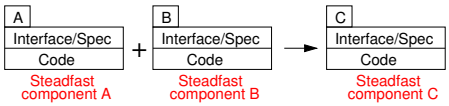

Fig. 10. Composing steadfast components.

in Figure 10.

In the context of modular specification and verification (as shown in Figure 4), steadfast modules can be verified and the specification of the composite can be predicted, prior to composition. This is illustrated in Figure 11. We understand that current

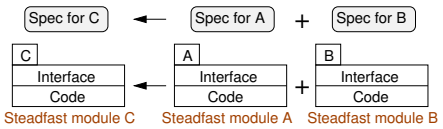

Fig. 11. Composing steadfast modules.

approaches to modular reasoning need to know the specification of the composite before predicting if the composite will work according to its specification. If this is the case (as shown in Figure 4), then steadfastness offers the advantage of being able to predict the specification of the composite prior to composition. Thus, with steadfast modules, we can do system prediction as shown in Figure 10.

13 Conclusion

For lack of space, we have presented the intuition behind steadfastness, to illustrate the notion of a priori correctness, by means of simple examples. We hope this does not detract from the presentation of our idea of a priori reasoning. A full account of steadfastness can be found in [8]. Steadfastness is defined in terms of model-theoretic semantics. It is thus declarative in nature. We believe that declarative semantics in general will be important for lifting the level of abstraction, necessary for a shift in paradigm to a priori reasoning.

Our approach to specifying components is very generic. The component may be just a class or ADT. It may be a module, in particular what Meyer [10] calls an *abstracted module*, which is the basic unit of reuse in the CBD methodology RESOLVE [14]. It may be an object model [2] as in OMT [11] or UML [12]. It may yet be an

OOD framework, i.e. a group of interacting objects [6], such as frameworks in the CBD methodology *Catalysis* [3, 5]. It could even be a design pattern or schema [4].

We believe that our approach to component specification can enable a priori reasoning, which we believe is important for CBD. In particular, as discussed in [7], we believe that a priori reasoning can deliver the key pre-requisites for CBD to achieve its ultimate goal of third-part assembly, these being:

- a *standard semantics* of components and component composition (and hence reuse);
- good (*component*) *interface specifications*;
- a good *assembly guide* for selecting the right components for building a specified system.

In addition, as also pointed out in [7], *a priori reasoning* can provide a hybrid, spiral approach to CBD that is both top-down and bottom-up for CBD, as illustrated in Figure 12. First a library of *a priori correct* components has to be built. The nature of *a*

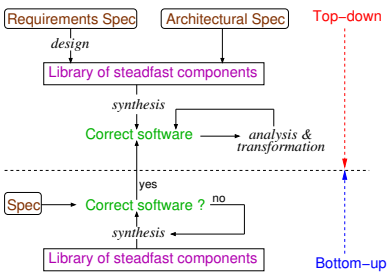

Fig. 12. A spiral model for CBD.

priori correctness, coupled with the use of *a priori reasoning*, then allows these components to be composed into larger systems in either a top-down (following the traditional *waterfall model* or the *software architecture* approach [13, 1]), or bottom-up manner, or indeed a combination of both.

Bottom-up development in particular is more in keeping with the spirit of CBD. Composition of a priori correct components can show the specification of the composite, and therefore the specification of any software constructed can be compared with the initial specification for the whole system. Guidance as to which components to 'pick and mix' can also be provided by component specifications.

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