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# DAML+OIL: a Reason-able Web Ontology Language

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Manchester, UK

# Talk Outline

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## The Semantic Web

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**Web Ontology Languages**

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**Summary**

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- ➔ In **next generation** web, **resources** should be more accessible to automated processes
  - To be achieved via **semantic markup**
  - **Metadata** annotations that describe content/function
- ➔ Coincides with Tim Berners-Lee's vision of a **Semantic Web**

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- ☞ Even partial realisation will be a **major undertaking**
- ☞ Input will be required from **many communities**
- ☞ E.g., topics covered at **ISWC** include:

Agents

Database technologies

Digital libraries

e-business

e-science and the Grid

Integration, mediation and storage

Knowledge representation and reasoning

Languages and infrastructure

Metadata (inc. generation and authoring)

Multimedia data

Natural language

Ontologies

Searching and querying

Services and service description

Trust and meaning

User interfaces

Visualisation and modelling

Web mining



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- ➔ Degree of formality can be quite variable (NL–logic)
- ➔ Increased formality and regularity facilitates machine understanding
- ➔ Ontologies can be used, e.g.:
  - To facilitate buyer–seller communication in **e-commerce**
  - In semantic based **search**
  - To provide richer **service descriptions** that can be more flexibly interpreted by intelligent agents

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# Web Ontology Languages



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- ➔ But RDFS not a suitable foundation for Semantic Web
  - **Too weak** to describe resources in sufficient detail
- ➔ Requirements for web ontology language:
  - **Compatible** with existing Web standards (XML, RDF, RDFS)
  - **Easy to understand** and use (based on common KR idioms)
  - **Formally specified** and of “adequate” expressive power
  - Possible to provide **automated reasoning** support

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  - **DAML-ONT**: developed by group of (largely) US researchers (in DARPA DAML programme)
- ➔ Efforts merged to produce DAML+OIL
  - Development was overseen by **joint EU/US committee**
  - Now **submitted to W3C** as basis for standardisation
  - **WebOnt working group** developing language standard
  - New standard may be called **OWL** (Ontology Web Language)



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  - RDFS based **syntax**
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  - **Object oriented**: classes (concepts) and properties (roles)
  - DAML+OIL ontology consists of set of **axioms** asserting characteristics of classes and properties
  - E.g., Person is **kind of** Animal whose parents are Persons

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- ➔ RDF used for class/property membership assertions (**data**)
  - E.g., John is an **instance of** Person; ⟨John, Mary⟩ is an instance of parent

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# DAML+OIL Language

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- ➔ More precisely, DAML+OIL is (extension of) *SHIQ* DL
- ➔ DAML+OIL benefits from many years of DL research
  - Well defined **semantics**
  - **Formal properties** well understood (complexity, decidability)
  - Known **reasoning algorithms**
  - **Implemented systems** (highly optimised)

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- ➔ DAML+OIL classes can be names (URI's) or **expressions**
  - Various **constructors** provided for building class expressions
- ➔ **Expressive power** determined by
  - Kinds of constructor provided
  - Kinds of axiom allowed

# DAML+OIL Class Constructors

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Constructor	DL Syntax	Example
intersectionOf	$C_1 \sqcap \dots \sqcap C_n$	Human $\sqcap$ Male
unionOf	$C_1 \sqcup \dots \sqcup C_n$	Doctor $\sqcup$ Lawyer
complementOf	$\neg C$	$\neg$ Male
oneOf	$\{x_1 \dots x_n\}$	{john, mary}
toClass	$\forall P.C$	$\forall$ hasChild.Doctor
hasClass	$\exists P.C$	$\exists$ hasChild.Lawyer
hasValue	$\exists P.\{x\}$	$\exists$ citizenOf.{USA}
minCardinalityQ	$\geq n P.C$	$\geq 2$ hasChild.Lawyer
maxCardinalityQ	$\leq n P.C$	$\leq 1$ hasChild.Male
cardinalityQ	$= n P.C$	$= 1$ hasParent.Female

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- ➔ XMLS **datatypes** as well as classes
- ➔ Arbitrarily complex **nesting** of constructors
  - E.g., Person  $\sqcap \forall$ hasChild.(Doctor  $\sqcup \exists$ hasChild.Doctor)



# RDFS Syntax

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```
<daml:Class>
  <daml:intersectionOf rdf:parseType="daml:collection">
    <daml:Class rdf:about="#Person" />
    <daml:Restriction>
      <daml:onProperty rdf:resource="#hasChild" />
      <daml:toClass>
        <daml:unionOf rdf:parseType="daml:collection">
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sameClassAs	$C_1 \equiv C_2$	Man $\equiv$ Human $\sqcap$ Male
subPropertyOf	$P_1 \sqsubseteq P_2$	hasDaughter $\sqsubseteq$ hasChild
samePropertyAs	$P_1 \equiv P_2$	cost $\equiv$ price
sameIndividualAs	$\{x_1\} \equiv \{x_2\}$	{President_Bush} $\equiv$ {G_W_Bush}
disjointWith	$C_1 \sqsubseteq \neg C_2$	Male $\sqsubseteq \neg$ Female
differentIndividualFrom	$\{x_1\} \sqsubseteq \neg\{x_2\}$	{john} $\sqsubseteq \neg\{peter\}$
inverseOf	$P_1 \equiv P_2^-$	hasChild $\equiv$ hasParent <sup>-</sup>
transitiveProperty	$P^+ \sqsubseteq P$	ancestor <sup>+</sup> $\sqsubseteq$ ancestor
uniqueProperty	$\top \sqsubseteq \leq 1P$	$\top \sqsubseteq \leq 1$ hasMother
unambiguousProperty	$\top \sqsubseteq \leq 1P^-$	$\top \sqsubseteq \leq 1$ isMotherOf <sup>-</sup>

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➡ Axioms (mostly) **reducible to subClass/PropertyOf**

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- ➔ In practice, DAML+OIL implementations can choose to support **subset** of XML Schema datatypes.

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# Reasoning with DAML+OIL

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- ➔ Ontology **deployment**
  - Determine if set of facts are consistent w.r.t. ontology
  - Determine if individuals are instances of ontology classes

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  - XML provides syntax **transport layer**
  - RDF(S) provides basic **relational language** and simple ontological primitives
  - DAML+OIL provides powerful but still decidable **ontology language**
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  - Known “practical” **algorithms**
  - Several implemented **systems**
  - Evidence of **empirical tractability**

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  - Evidence of **empirical tractability**
- ➔ Understanding dependent on **reliable & consistent** reasoning

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- Is  $\mathcal{O}$  consistent?    There exists some model  $\mathcal{I}$  of  $\mathcal{O}$
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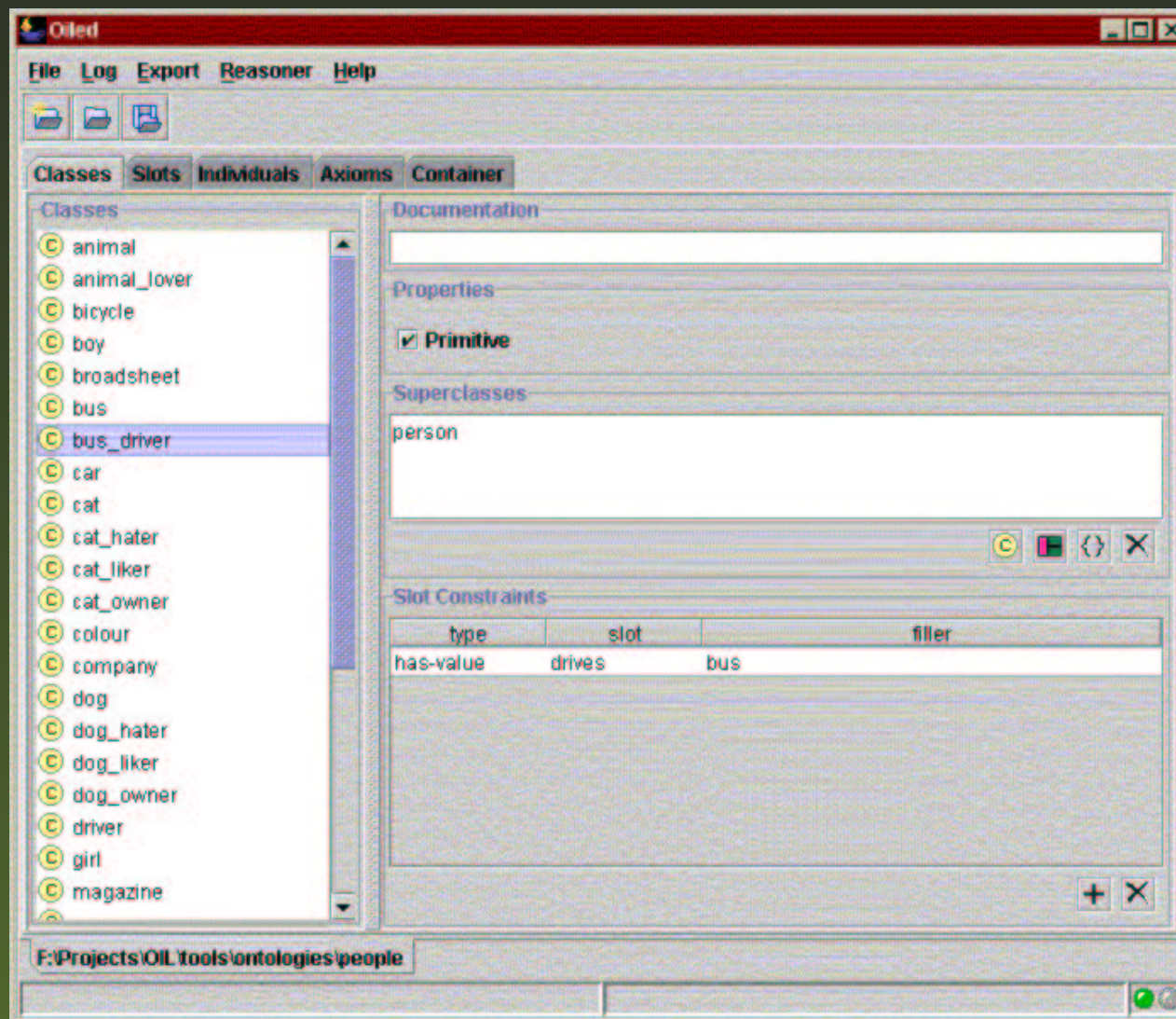
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☞ Problems all **reducible** to consistency (satisfiability):

- $C \sqsubseteq_{\mathcal{O}} D$  iff  $D \sqcap \neg C$  not consistent w.r.t.  $\mathcal{O}$
- $i \in_{\mathcal{O}} C$  iff  $\mathcal{O} \cup \{i \in \neg C\}$  is **not** consistent

# Reasoning Support for Ontology Design: OilEd



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# Description Logic Reasoning

# Highly Optimised Implementation

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👉 Naive implementation  $\longrightarrow$  effective non-termination

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  - Use structural information to select classification order
- ➔ Optimised **subsumption** testing (search for models)
  - Normalisation and simplification of concepts
  - Absorption (simplification) of general axioms
  - Davis-Putnam style semantic branching search
  - Dependency directed backtracking
  - Caching of satisfiability results and (partial) models
  - Heuristic ordering of propositional and modal expansion
  - ...

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- ➔ Already seeing some (partial) **implementations**
  - Cerebra system (Network Inference), Racer system (Hamburg)

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  - Promising research on **automata** based algorithms
- ➔ **Standard solution** is weaker semantics for nominals
  - Treat nominals as (disjoint) primitive classes
  - Loose some inferential power, e.g., w.r.t. max cardinality

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- ➔ **Problems** can arise when  $SHF$  extended to  $SHIQ$ 
  - Important **optimisations** no longer (fully) work
- ➔ Reasoning with **individuals**
  - **Deployment** of web ontologies will mean reasoning with (possibly very large numbers of) individuals/tuples
  - Unlikely that standard **Abox** techniques will be able to cope
  - Necessary to employ **database** technology

# Other Reasoning Tasks

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## Querying

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## 👉 LCS and/or matching [Baader, Küsters & Molitor]

- To support ontology integration
- To support “bottom up” design of ontologies

# Tools and Infrastructure

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## ☞ Ontology **design and maintenance**

- Several **editors** available, e.g, OilEd (Manchester), OntoEdit (Karlsruhe), Protégé (Stanford)
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  - Formal rigor of Description Logic
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- **Popular** combination of features—already being widely adopted
- **Challenges** remain
  - Reasoning with full language
  - Demonstration of scalability
  - Development of (high quality) tools and infrastructure

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- ➔ Members of the Information Management, Medical Informatics, Formal Methods and Artificial Intelligence Groups at the University of Manchester

# Resources

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Slides from this talk

<http://www.cs.man.ac.uk/~horrocks/Slides/caise02.pdf>

FaCT system (open source)

<http://www.cs.man.ac.uk/FaCT/>

OilEd (open source)

<http://oiled.man.ac.uk/>

OIL

<http://www.ontoknowledge.org/oil/>

DAML+OIL

<http://www.w3c.org/Submission/2001/12/>

I.COM (CASE tool with reasoning support)

[www.cs.man.ac.uk/~franconi/icom/](http://www.cs.man.ac.uk/~franconi/icom/)

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